

A MODEL FOR DORIS USO IN THE SAA

E. Jalabert, F. Mercier⁽¹⁾

June 11-12, 2018

Toulouse,
FRANCE

(1) CNES POD Team, Toulouse, France



INTRODUCTION

- DORIS measurements rely on the **precise knowledge** of the Ultra Stable **Oscillator** (DORIS USO)
- The important radiations in the **South Atlantic Anomaly** (SAA) **perturb the USO** behavior by causing rapid frequency variations
- If these variations are not modelled : **systematic errors**
- Goal : a **model** of the frequency variations due to the SAA
So far : on Jason3 and Sentinel3a

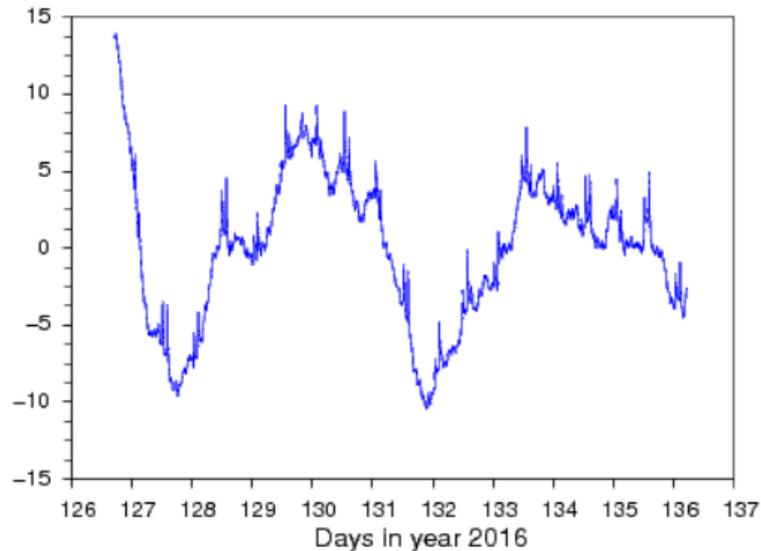
CONTENTS

- INTRODUCTION
- MODELLING
- RESULTS ON RMS
- RESULTS ON STATION POSITIONING
- CONCLUSION

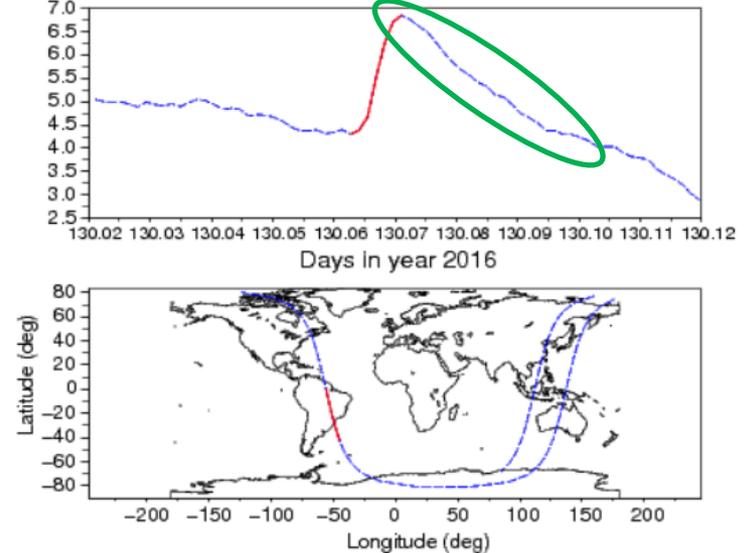
MODELLING : FREQUENCY BEHAVIOUR (1)

- Model based on observations of Sentinel3A USO

GPS clock (ns), w/o 4th order polynomial, with relativistic correction



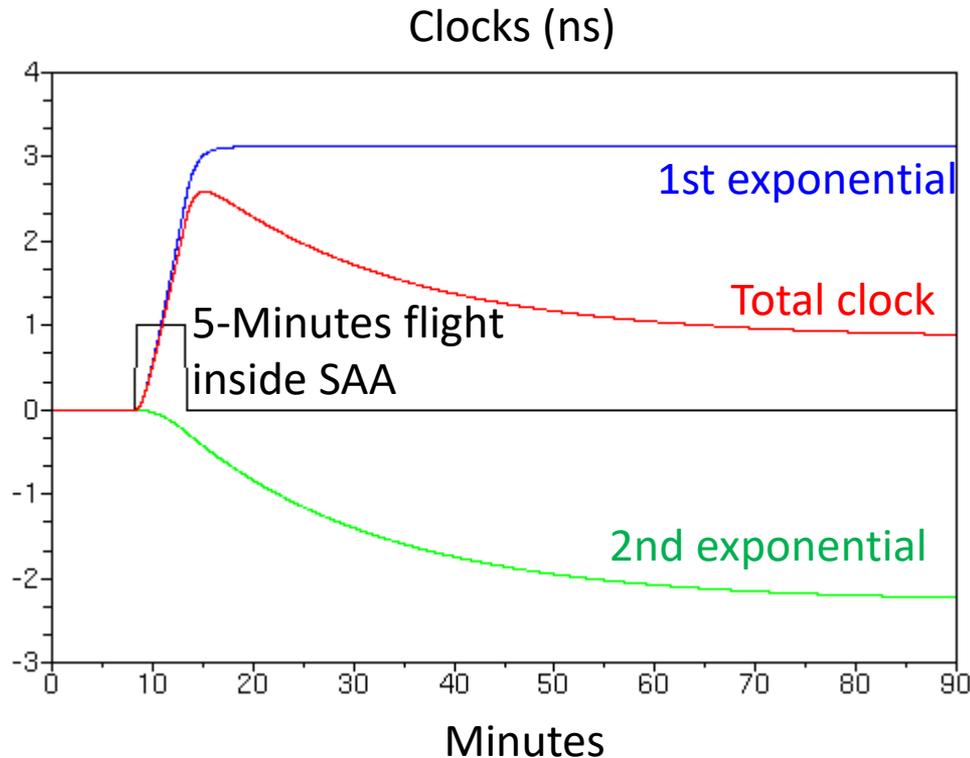
GPS clock (ns) w/o 4th order polynomial, with relativistic correction



- Two phenomenon :
 - **Drift** when entering the SAA
 - **Relaxation** after exiting the SAA

MODELLING : FREQUENCY BEHAVIOUR (2)

- In order to reproduce the behaviour observed on Sentinel3A USO, two exponentials are added :
 - One describing the drift when the satellite enters the SAA
 - One describing the relaxation of the USO



MODELLING : FREQUENCY BEHAVIOUR (3)

- Model : USO frequency f is the **sum of two exponentials**

$$\begin{aligned}df_1 &= -\alpha_1 f_1 + \beta_1 a(t) \\df_2 &= -\alpha_2 f_2 + \beta_2 a(t)\end{aligned}$$

With :

- $\alpha_i = 1/\tau_i$: inverse of the time constant of the exponentials
- $a(t)$: the radiation exposure due to the SAA at time t
- β_i : gain linked to the exposure

MODELLING : PARAMETERS (1)

- α_i : cannot be estimated
depends on the USO device
- Sentinel3a : the USO behaviour is known, and so are the **time constants**. (see « Analysis of South Atlantic Anomaly perturbations on Sentinel-3A Ultra Stable Oscillator. Impact on DORIS phase measurement and DORIS station positioning. » Jalabert and Mercier)
 - $\alpha_1 = 1$ minute
 - $\alpha_2 = 20$ minutes
- Jason3 : the hypothesis is that the time constants are similar to those of Jason1. The values are read on the plot **of the article** « A corrective model for Jason-1 DORIS Doppler data in relation to the South Atlantic Anomaly », JM Lemoine and H. Capdeville
 - $\alpha_1 = 1$ minute
 - $\alpha_2 = 90$ minutes

MODELLING : PARAMETERS (2)

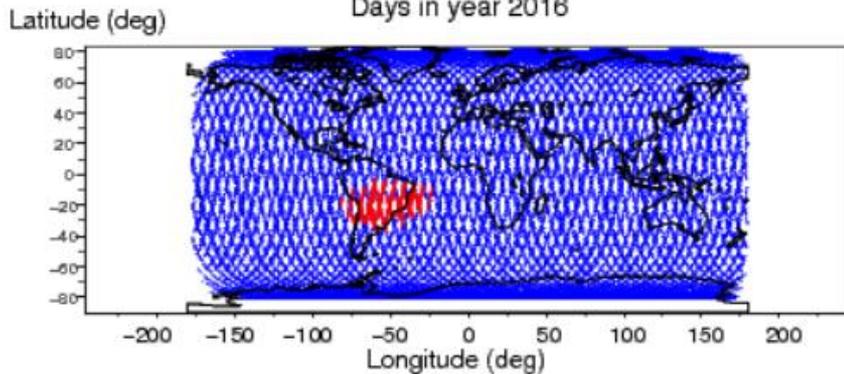
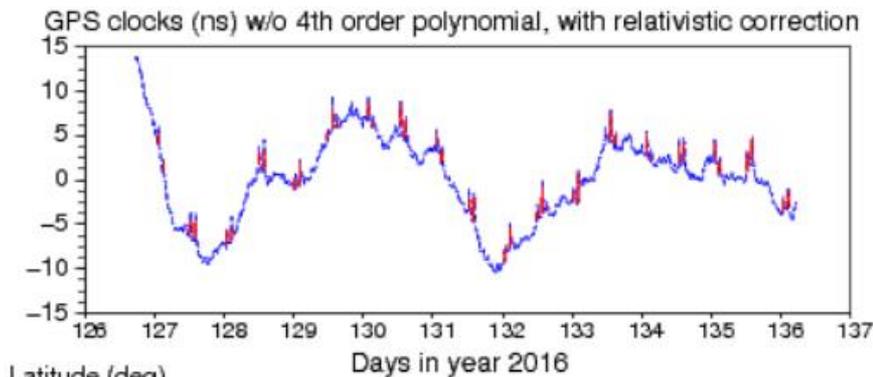
- β_i : estimated during the orbit determination process
- $a(t)$: geographical grid from the article « A corrective model for Jason-1 DORIS Doppler data in relation to the South Atlantic Anomaly », JM Lemoine and H. Capdeville

$$\exp\left(-\frac{1}{2}\left[\frac{\text{lat} - \text{lat}_{SAA}}{SAA_lat_extend}\right]^2\right) * \exp\left(-\frac{1}{2}\left[\frac{\text{lon} - \text{lon}_{SAA}}{SAA_lon_extend}\right]^2\right)$$

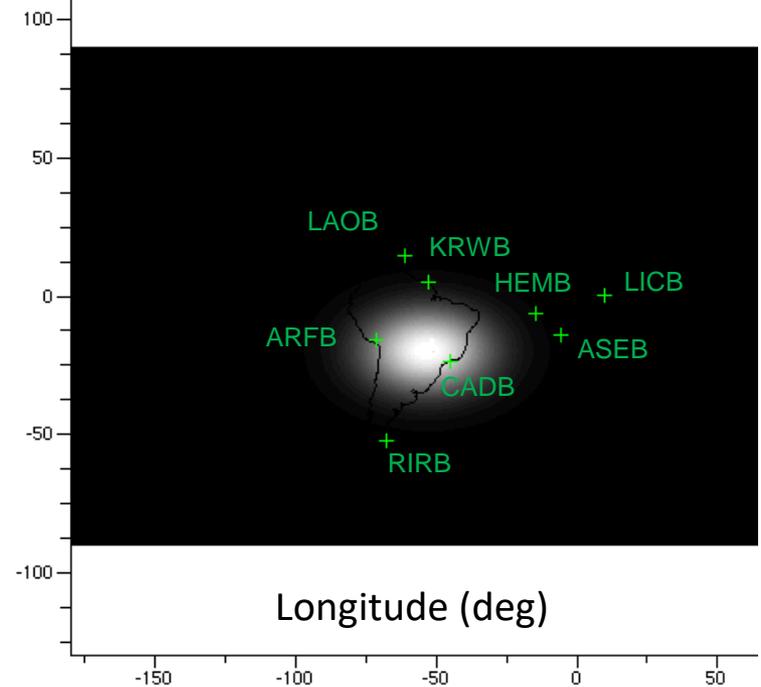
- The difficulty is to properly place the SAA on the Earth.
 - For Sentinel3a, the USO behaviour being known, it is straightforward.
 - But for Jason3, the SAA was placed empirically.

MODELLING : SENTINEL3A SAA GRID (1)

- The area where the drift in the USO occurs can be plotted.



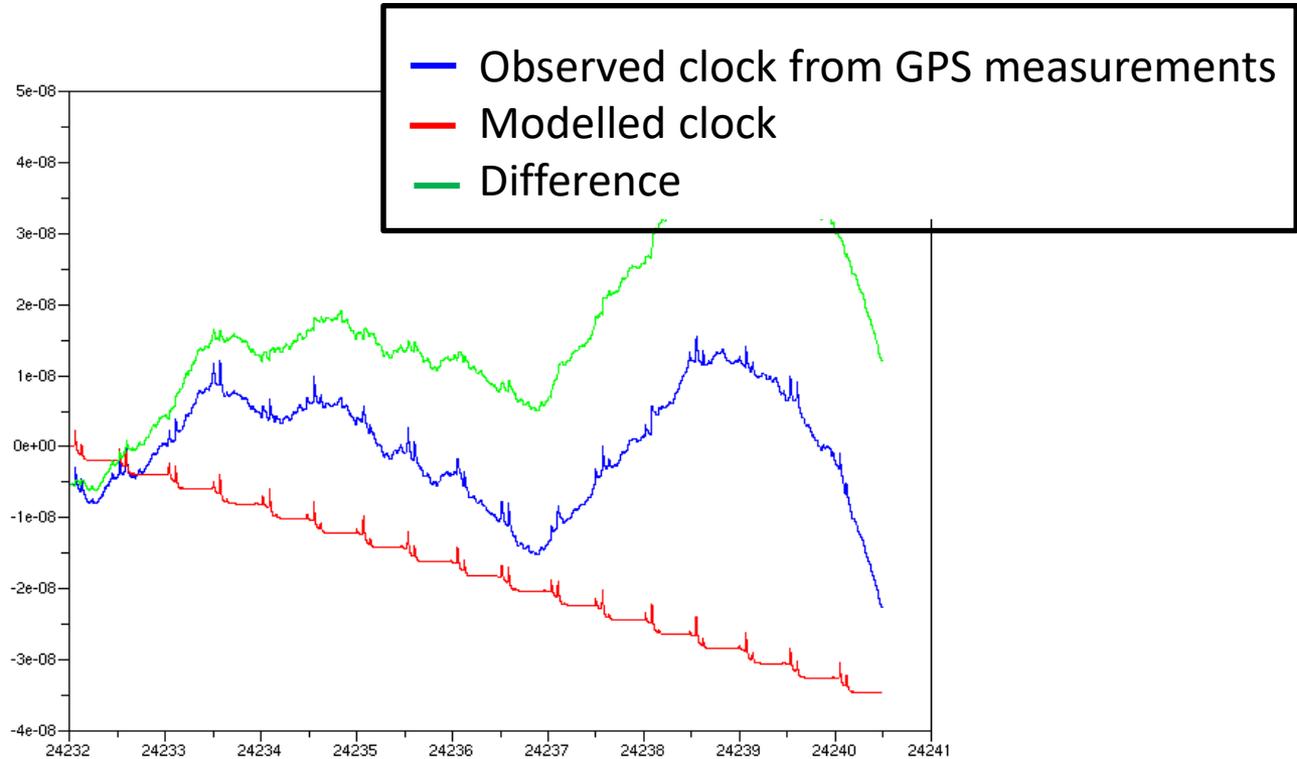
Latitude (deg)



```
milieuLongSAA=-53 ;  
milieuLatSAA=-20 ;  
envergureLong=15 ;  
envergureLat=10 ;  
A=0*%pi/180;
```

MODELLING : SENTINEL3A SAA GRID (2)

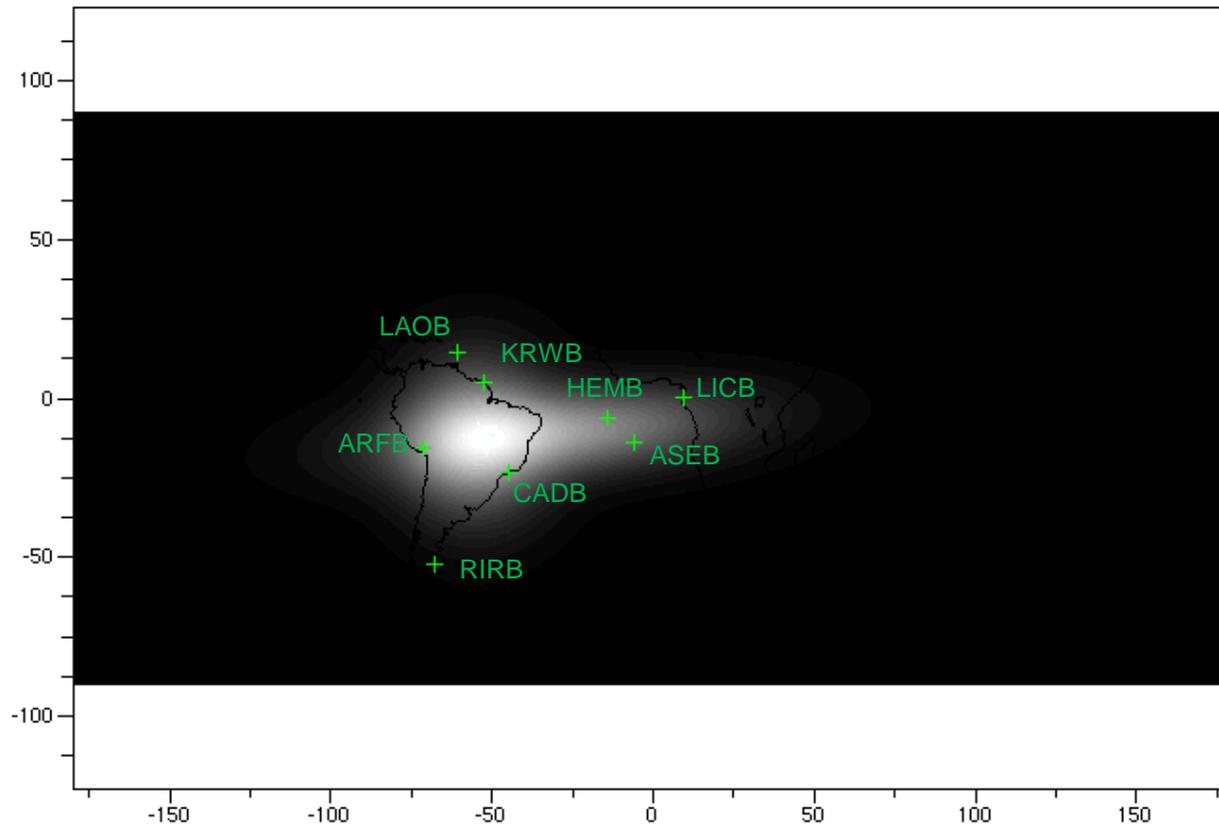
- The chosen positioning of the area is satisfying because it corrects the SAA peaks in the DORIS USO.



- Note : the drift coming from the integration of the model is small enough not to perturb the time tagging. (3×10^{-8} sec / 9 days, i.e 7mm over 1 pass)

MODELLING : JASON3 SAA GRID

- The positioning of the SAA area is empirical.
- Two ellipse are necessary to better represent the area.

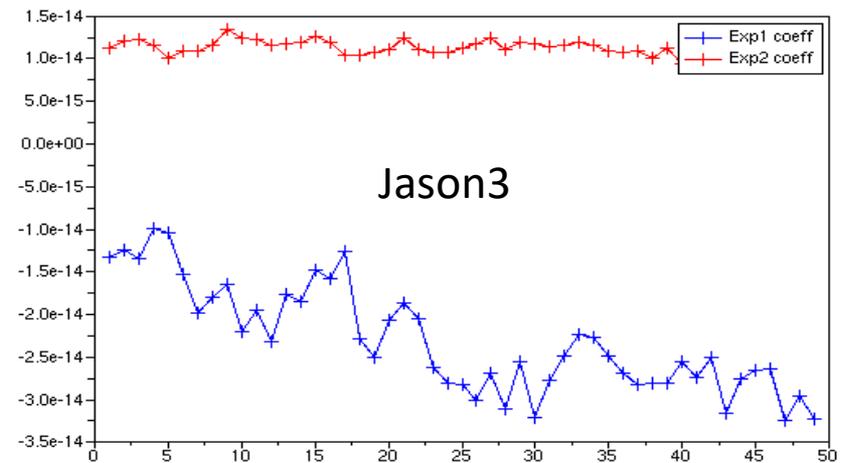
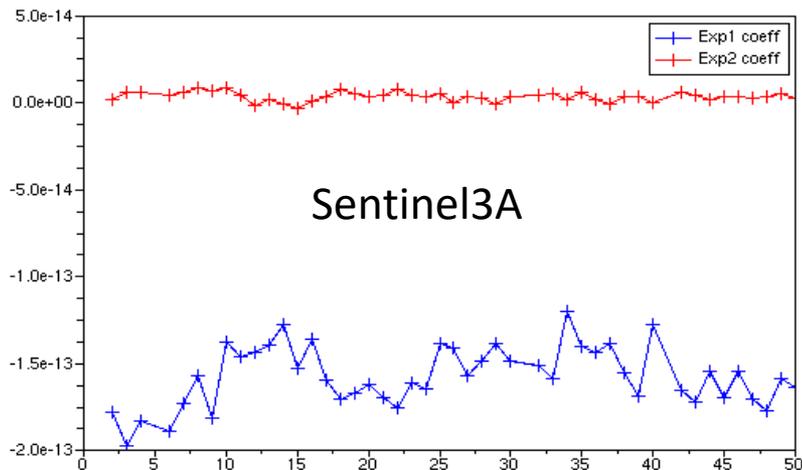


```
// 1er patch
milieulongSAA=-29 ;
milieulatSAA=-11 ;
envergurelong=36 ;
envergurelat=9 ;
A=-5*%pi/180;

// 2e patch
milieulongSAA2=-55 ;
milieulatSAA2=-13 ;
envergurelong2=15 ;
envergurelat2=17 ;
B=0*%pi/180;
```

MODELLING : GAIN ON EXPOSURE

- During the orbit determination process, only β_i are estimated. The other parameters for the model are fixed.
- Stable in time for β_2 (relaxation)
- Small and long term variations for β_1 (drift when entering the SAA)

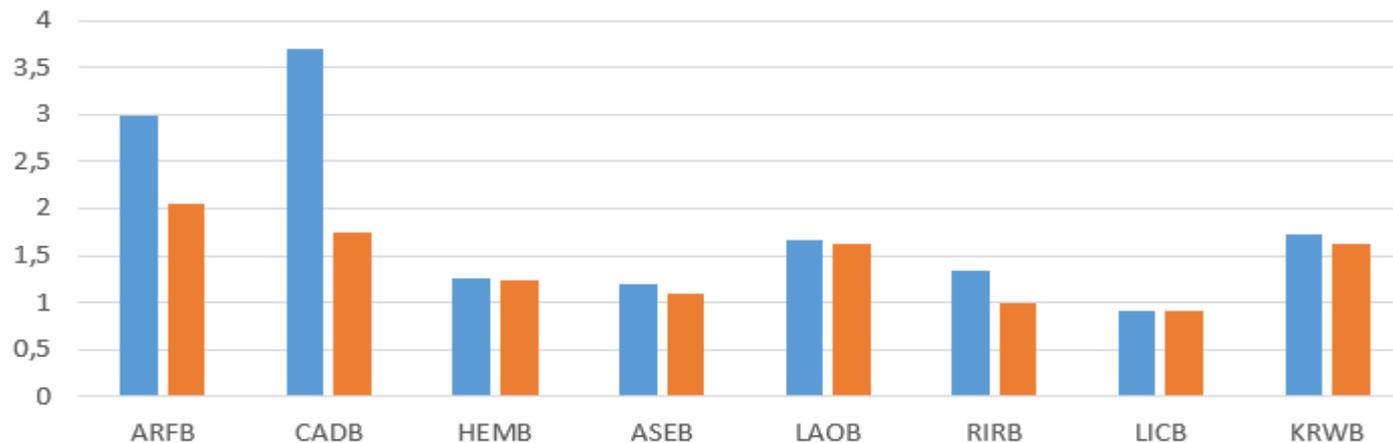


CONTENTS

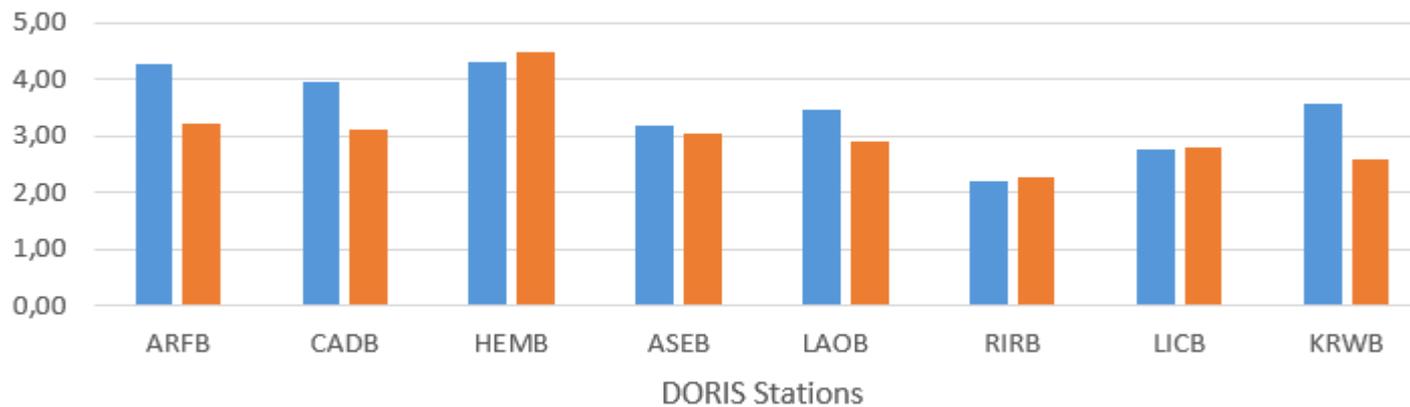
- INTRODUCTION
- MODELLING
- RESULTS ON RMS
- RESULTS ON STATION POSITIONING
- CONCLUSION

RESULTS ON RMS

Sentinel3A : Mean of the DORIS phase measurement RMS over ~40 cycles (cm)



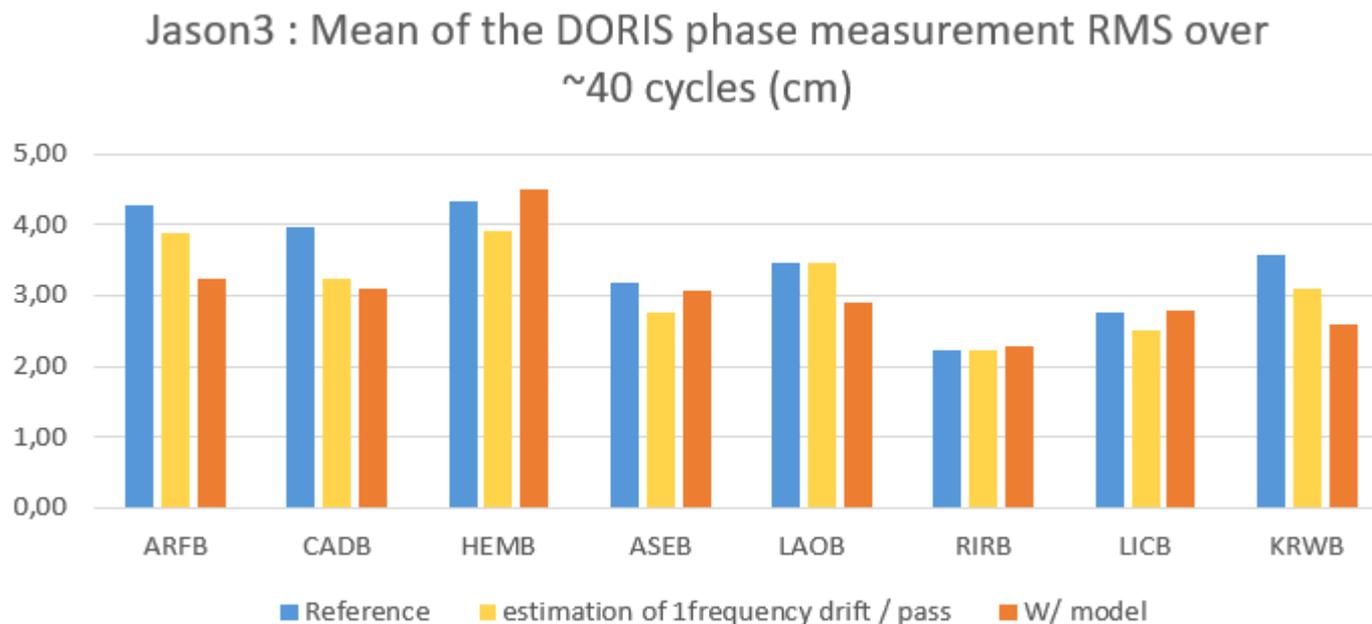
Jason3 : Mean of the DORIS phase measurement RMS over ~40 cycles (cm)



■ Reference ■ W/ model

RESULTS ON RMS

- OSTST 2016 : « band-aid » solution for SAA impact on Jason3 : estimation of a drift in frequency for each pass of stations inside the SAA area.
- Similar results, depends on station

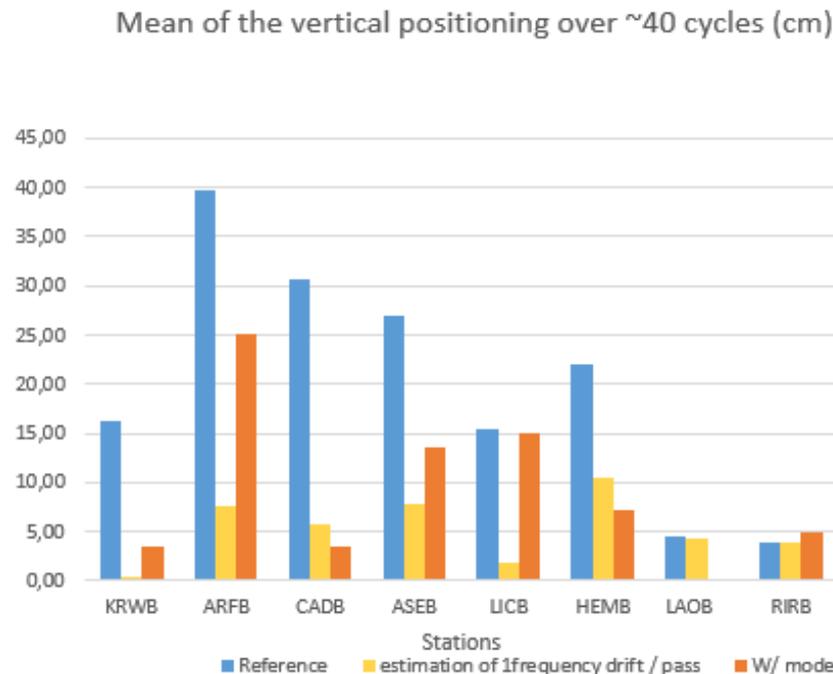


CONTENTS

- INTRODUCTION
- MODELLING
- RESULTS ON RMS
- RESULTS ON STATION POSITIONING
- CONCLUSION

RESULTS ON STATION POSITIONING (JASON3)

- The model enables to overall improve the vertical positioning. But it does not improve it as much as the « band-aid » solution presented at OSTST 2016.
- However, the model represents better the actual behaviour of the USO, rather than just estimating parabolic parameter on the clock, each pass, to minimise signatures.



CONTENTS

- INTRODUCTION
- MODELLING
- RESULTS ON RMS
- RESULTS ON STATION POSITIONING
- CONCLUSION

CONCLUSION

The modelling of SAA frequency variations enables to **improve DORIS phase measurement RMS** for stations in the SAA for SentinelA3 and Jason3.

It also **improves station positioning for Jason3**.

To do :

- Improve the SAA area definition on Jason3
- Apply the model on Jason 1