



CENTRE NATIONAL D'ÉTUDES SPATIALES

# Analysis of Jason-2 doris phase residuals and related POD results

F. Mercier, L. Cerri  
CNES

# Jason-2 new measurements types

Double-frequency synchronous phase and pseudo-range measurements (L1,C1 : 2 GHz    L2,C2 : 400 MHz)

10 sec. sampling

10 sec. + 3 sec. sample (not used here)

## Pseudo-range measurements , for time-tagging

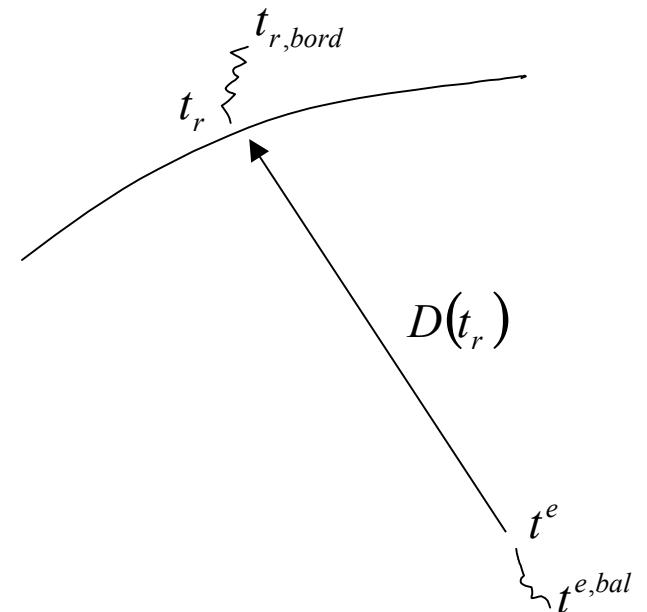
$$t_{r,bord} = t_r + h_r$$

propagation, including tropospheric effects

$$t^{e,bal} = t_r - \frac{D(t_r)}{c} + h^e$$

$$C = c(t_{r,bord} - t^{e,bal}) = D(t_r) + c(h_r - h^e)$$

pseudo-range



Time-tagging method used by CNES POD Team :

- preliminary orbit
- $h^e$  is known on reference beacons
- $t_{r,bord}$  is also known (on board time on Rinex files)
- $h_r$  is solved-for as polynomial (implicit form)

$$D(t_{r,bord} - h_r) + c(h_r - h^e) = C$$

Measurement :  
either C1 or C2, or  
iono-free  
combination

# Pseudo-range residual example

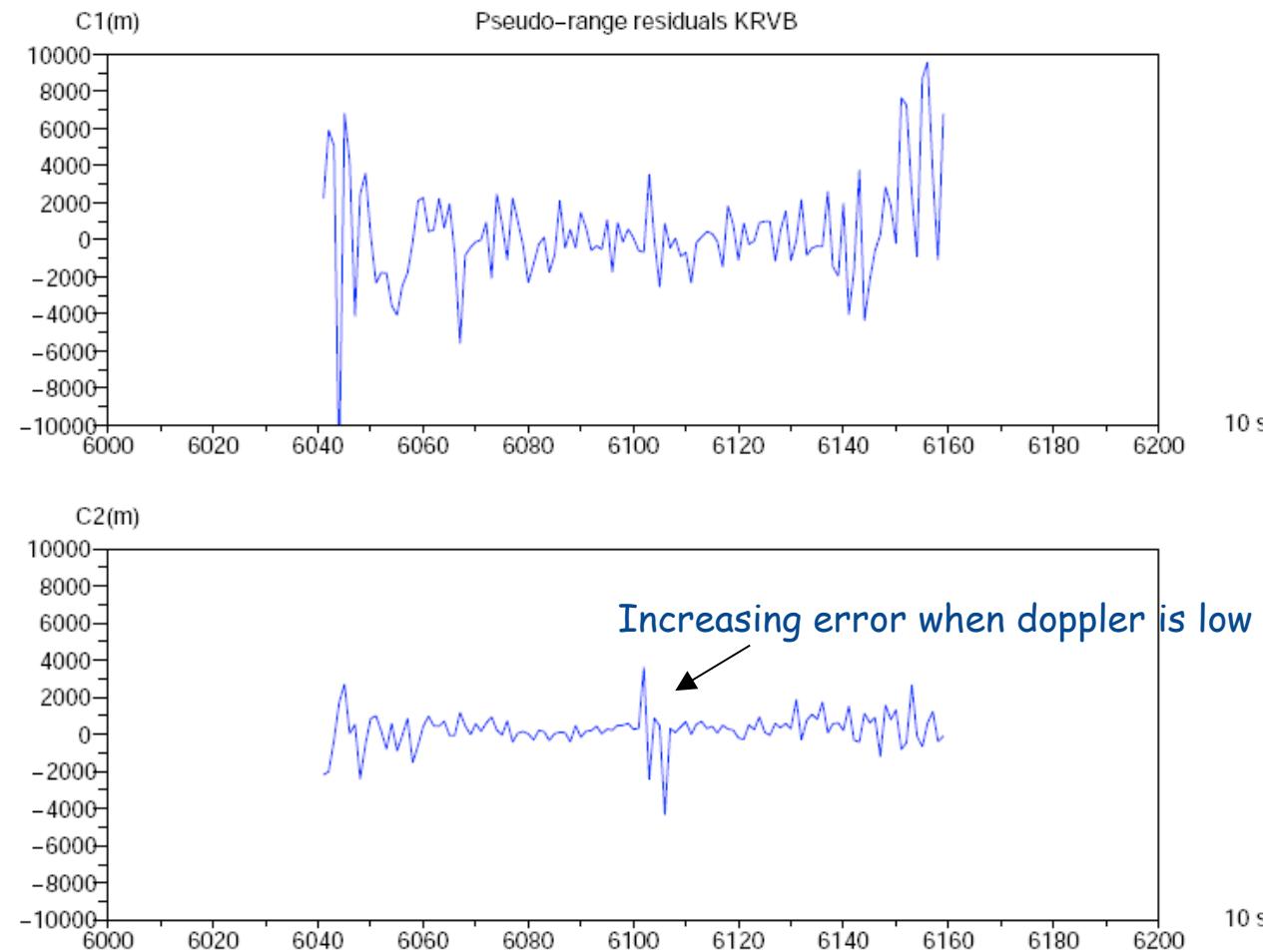


Figure 1: Pseudo-range residuals, sampling 10 seconds

# Phase measurements

Phase measurements, synchronous at the satellite phase centre

$$\begin{aligned}\lambda_1 L_1 &= D_{1,w}(t_r) - e + c(h_r - h^{e1}) - \lambda_1 N_1 \\ \lambda_2 L_2 &= D_{2,w}(t_r) - \gamma e + c(h_r - h^{e2}) - \lambda_2 N_2\end{aligned}$$

propagation, including troposphere,  
and windup

Beacon and receiver clocks

- Useful equations to detect cycle slips (integer variations of N1 and N2 within the same pass)
- Use the receiving time  $t_r = t_{r,bord} - h_r$  to model the distance and time-tagging polynom for the term  $ch_r$  (long term clock behaviour of receiver)
- In practice for orbit determination and station positioning, we process the iono-free observable, including a polynomial per pass to account for additional clock errors and ambiguities:

$$\frac{\gamma \lambda_1 L_1 - \lambda_2 L_2}{\gamma - 1} = D_{c,w}(t_r) + ch_r + a_0 + a_1 t + \dots + c(\delta h_r - \delta h^e) \leftarrow \text{Residual clock errors}$$

↑                      ↑                      ↑

Geometric model and troposphere              Long term on board  
clock model              Beacon/On-boards clocks at the pass time-scale  
and N1,N2 ambiguities (degree 1 is minimum degree for the polynomial)

# Phase measurements interruption, Doppler collisions

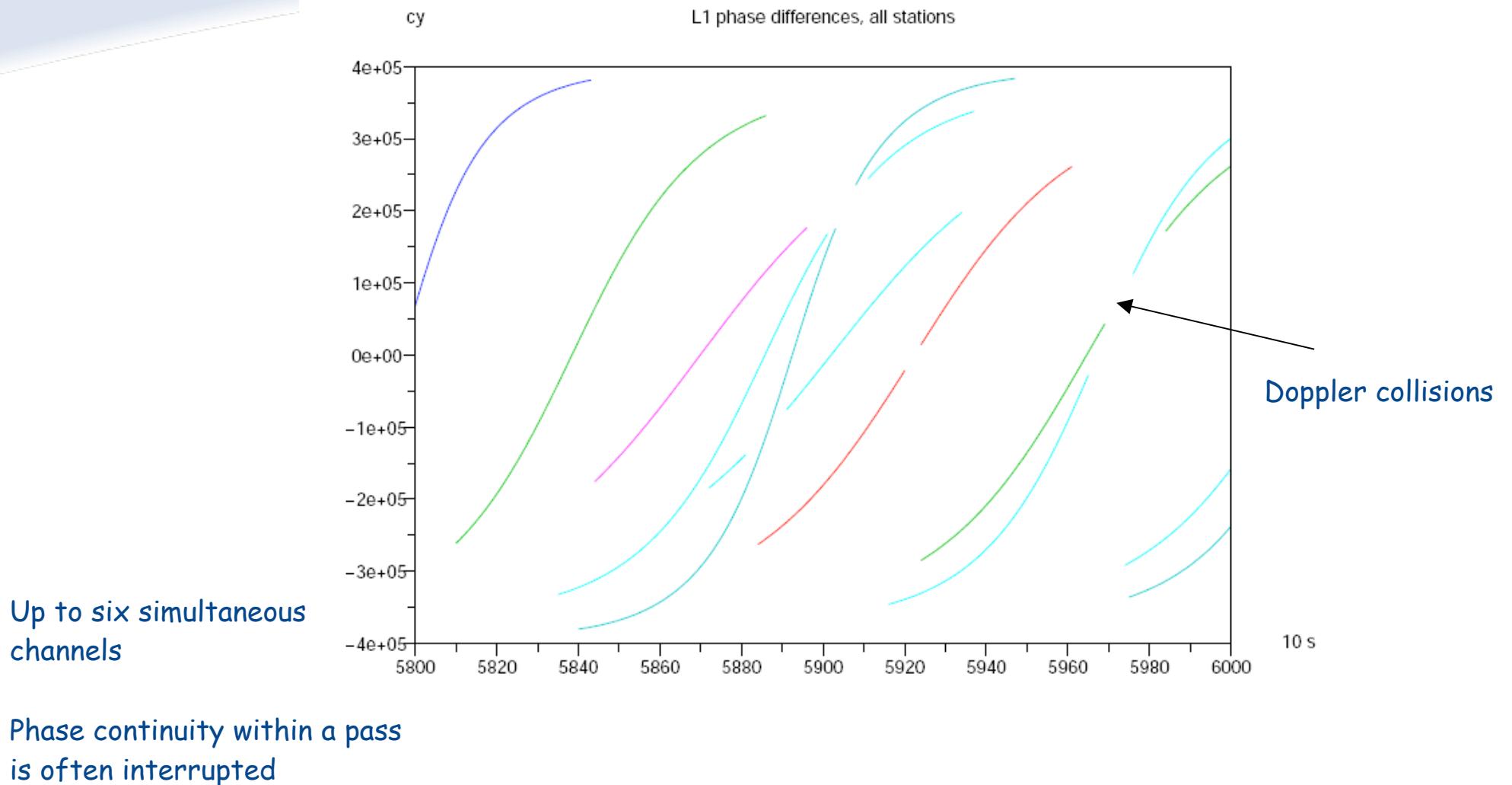


Figure 3:  $L_1$  time variations, sampling 10 seconds

# Phase measurements example, near-zero doppler measurements

Presence of cycle slips  
(mainly on L1)

At low elevation and near-zero  
doppler

Can be detected and fixed (see  
backups slides)

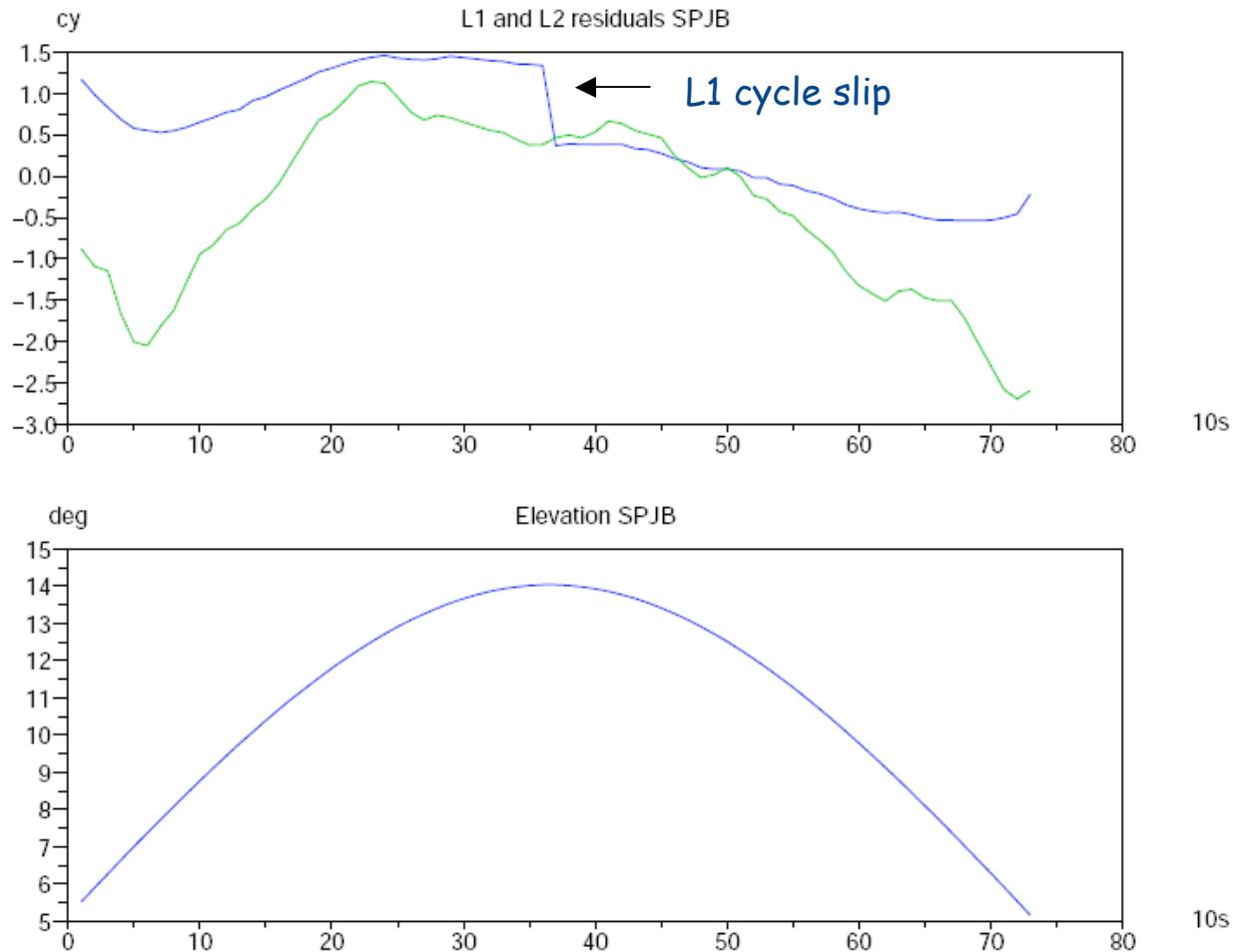
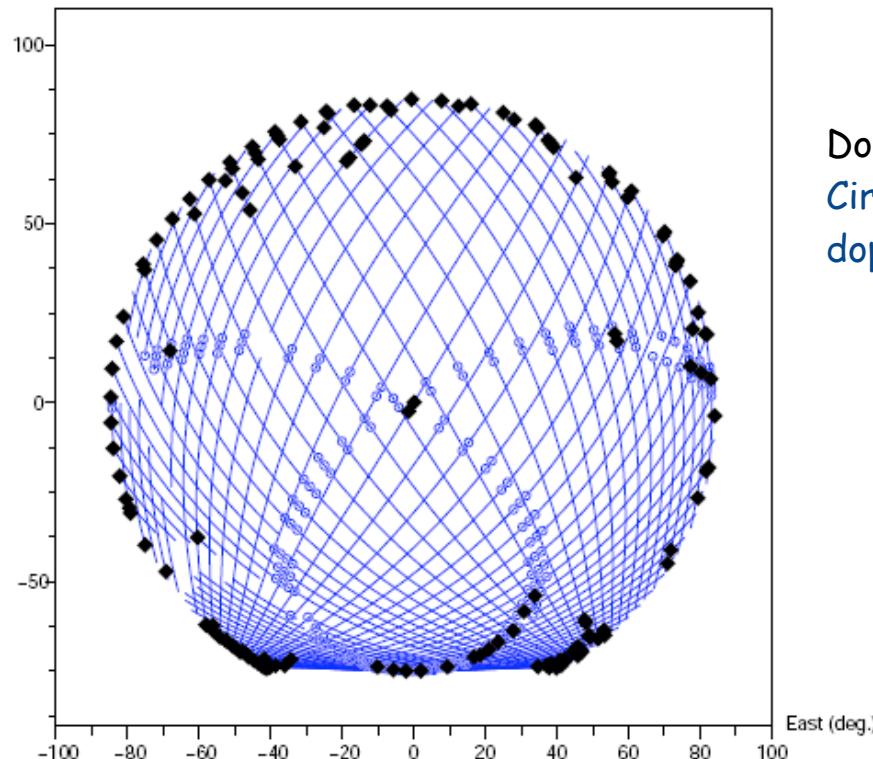


Figure 4: L1 residuals : one pass Jason2 station SPJB

# Cycle-slip reconstruction (CHAB)

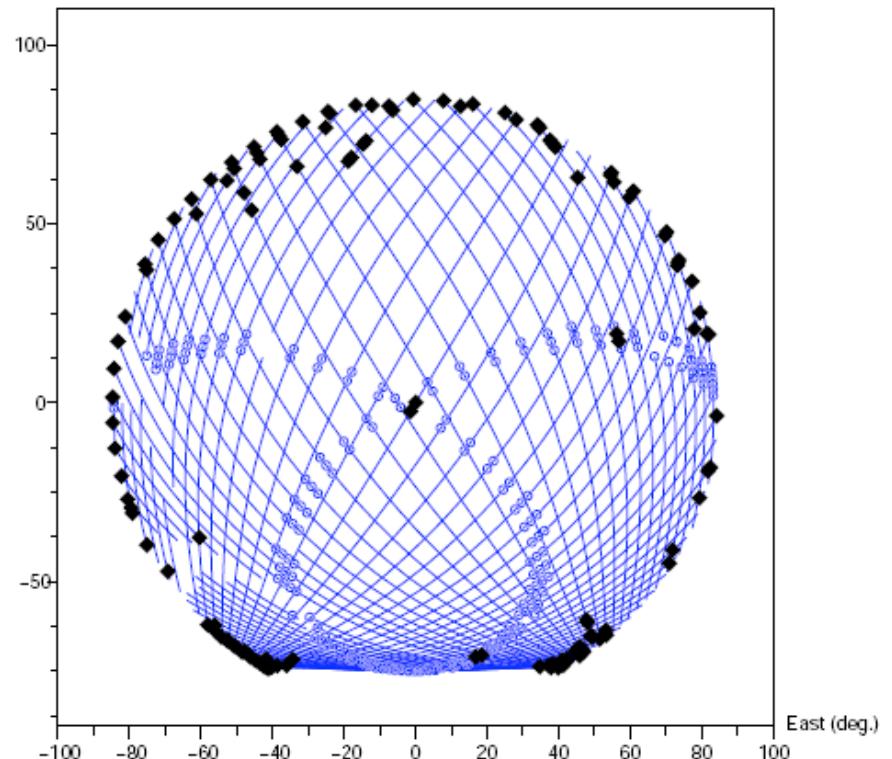
North (deg)

Cycle slips CHAB



North (deg)

Cycle slips CHAB



Dots: cycle slip  
Circles: near-zero  
doppler (<310 m/s)

Figure 5: Cycle slips station CHAB, without and with reconstruction

# Phase residuals analysis and antenna phase maps

## Method :

Eliminate the contribution of clock error : possible if many repeat cycles are processed

Cycle slip reconstruction to minimise pass brakes

Phase processing allows direct comparison of residuals and building of real phase maps.

In the case of Doppler, one has only access to the derivative along the ground track.  
Residuals are usually separated between ascending and descending tracks to avoid the handling of ground-tracks intersections.

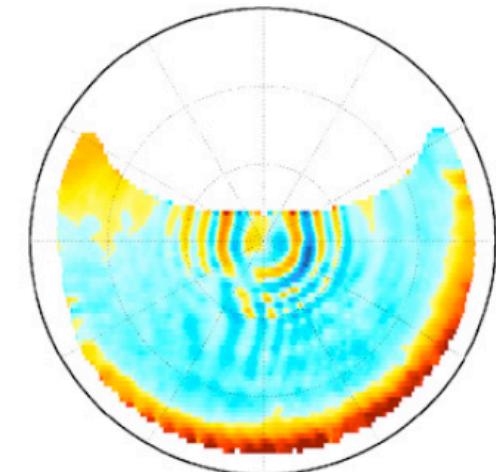
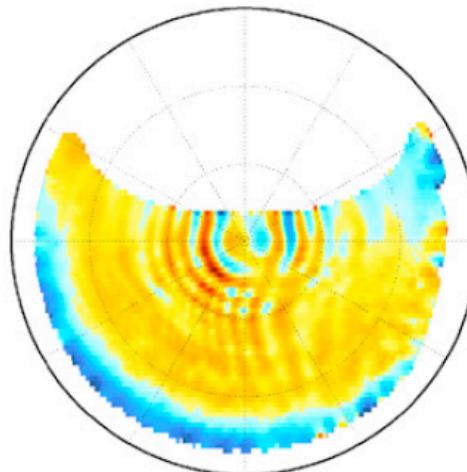


Phase residuals maps have been built for almost all the network

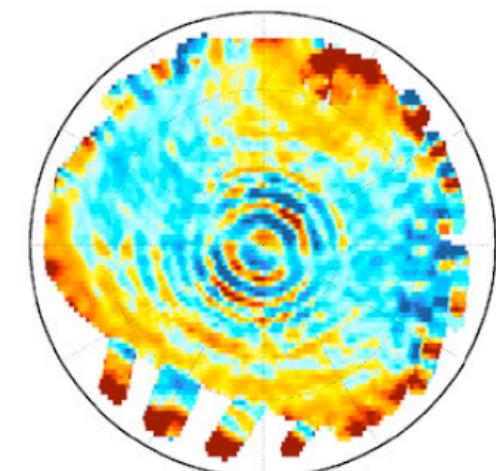
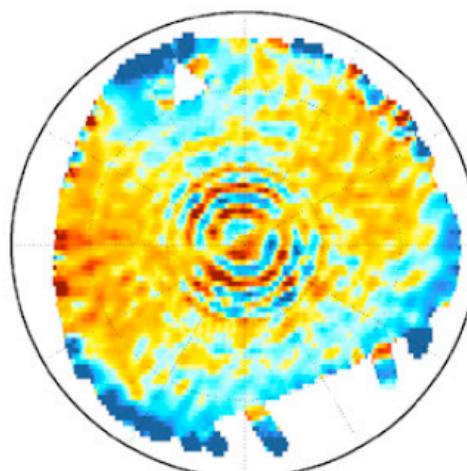
# Known doppler results on Fairbanks

Need to distinguish ascending from descending tracks, to avoid pass intersection. Difficult to handle high latitude stations on Jason orbit

Jason



Envisat



-0.6 -0.3 0.0 0.3 0.6

Mean [mm/s]

publication : E. Doornbos, P. Willis, Acta Astronautica

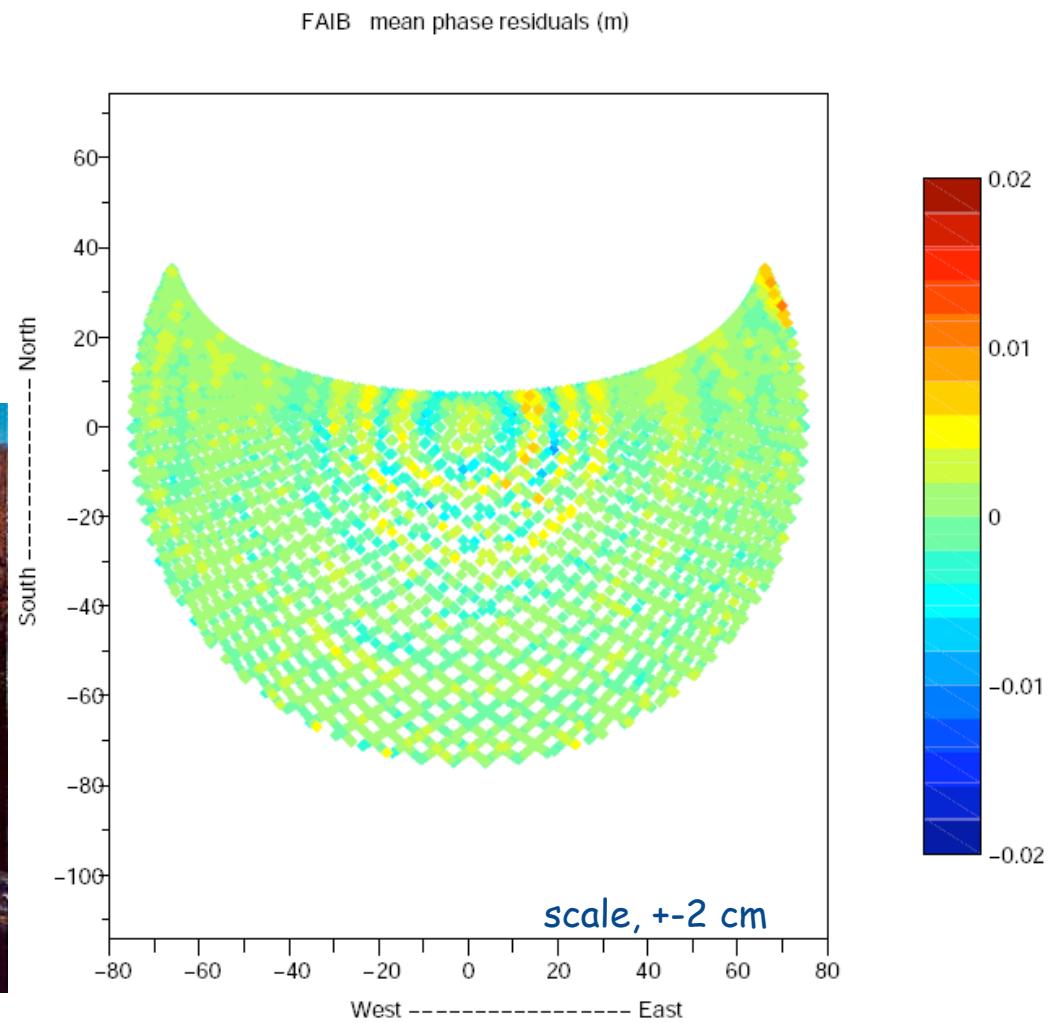
# Fairbanks phase map

Plot of the Jason-2 phase residuals over each mean pass. The mean was established over cycles 1-17

Interference ring pattern is clearly visible and very regular

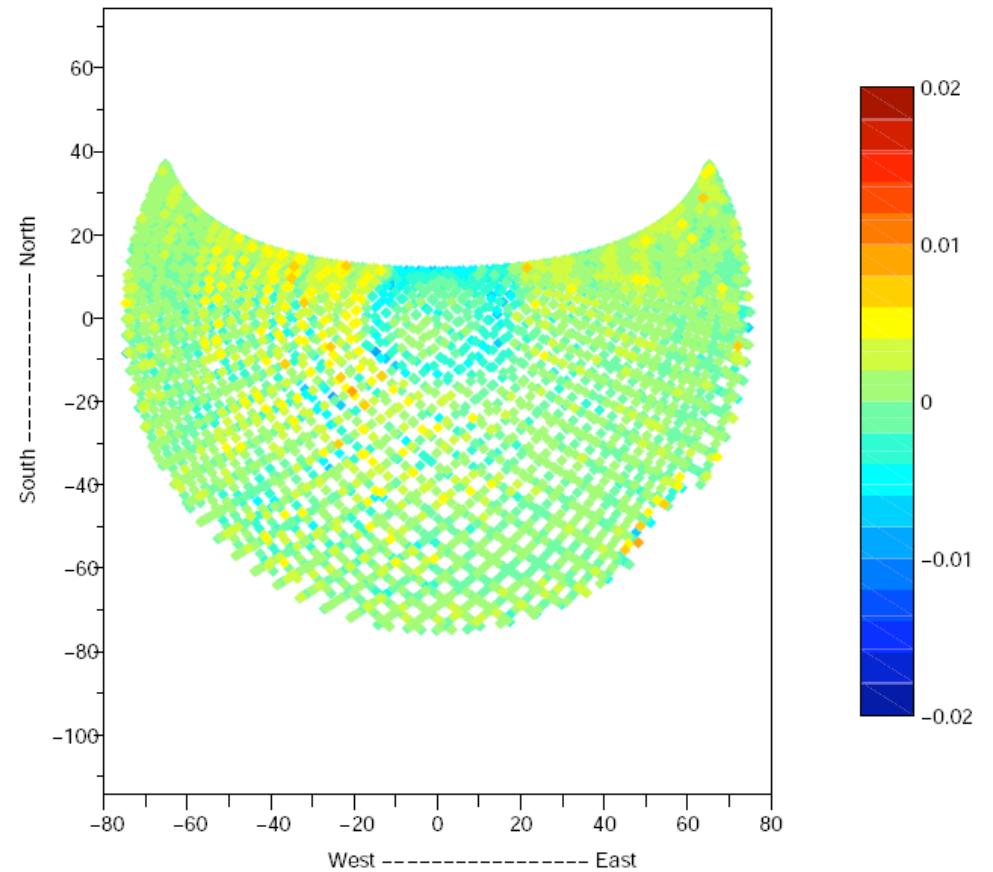


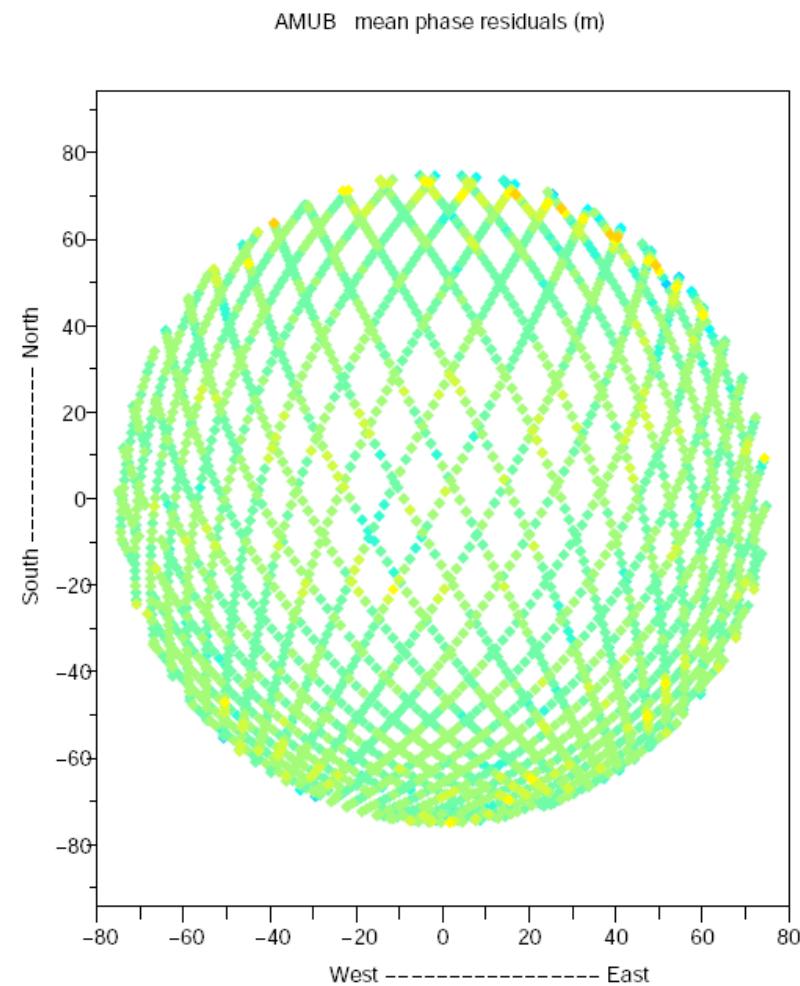
Site IDS : <http://ids.cls.fr/html/doris/stations/station.php?code=FAIB>





REZB mean phase residuals (m)





## More details on the processing of residuals used to obtain phase maps

Adjusted parameters per each visibility:

- 1 ambiguity per continuous phase measurement subset
- 1 wet tropospheric zenith delay
- 1 degree 3 polynomial

Measurements are synchronized with respect to the beginning of the cycle and the mean is performed over the corresponding passes of each cycle

# Residuals per pass

Residuals after  
adjustment of :  
- troposphere bias  
- degree 1 polynomial  
- ambiguities

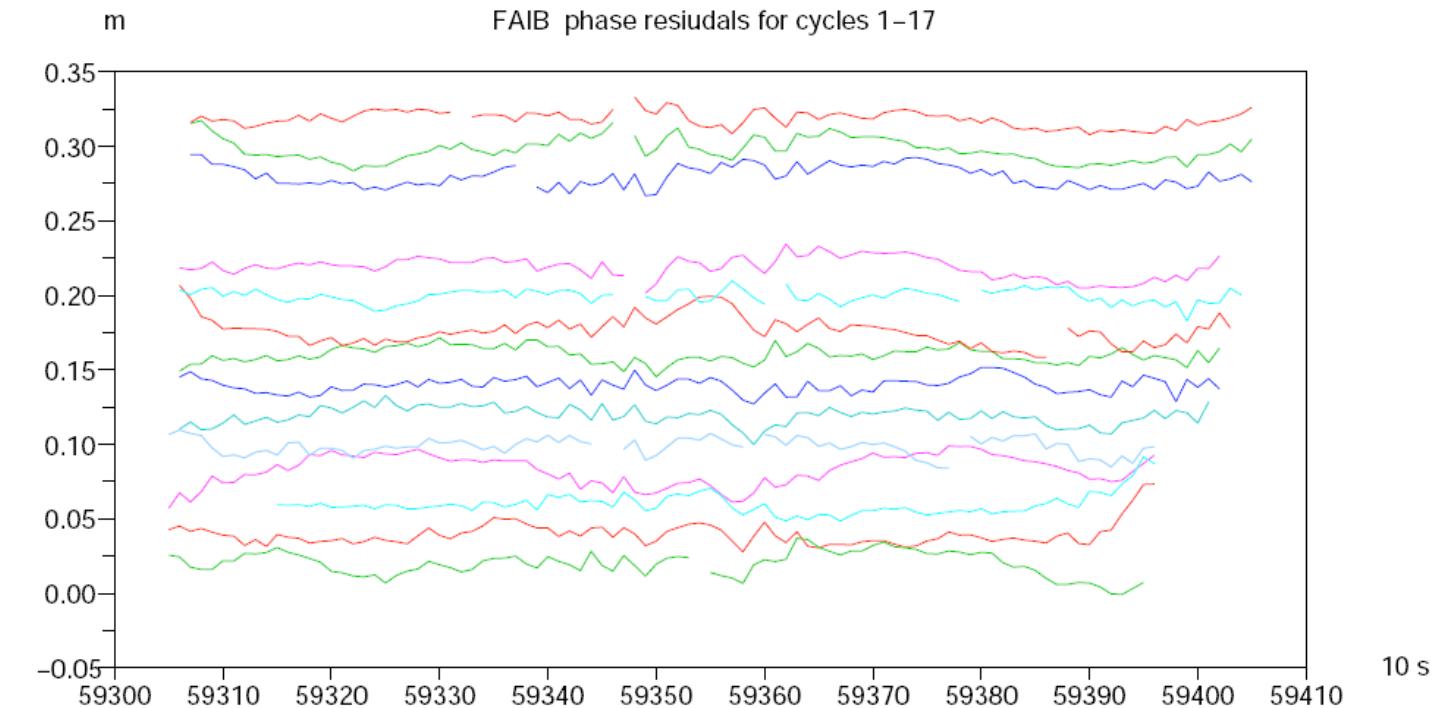


Figure 7: FAIB phase residuals for cycles 1-17, 2 cm offset added for each cycle

Short term oscillation are repeatable from one cycle to the other (phase maps)

Low frequency fluctuations (clock ?) --> need higher degree for polynomial (3)

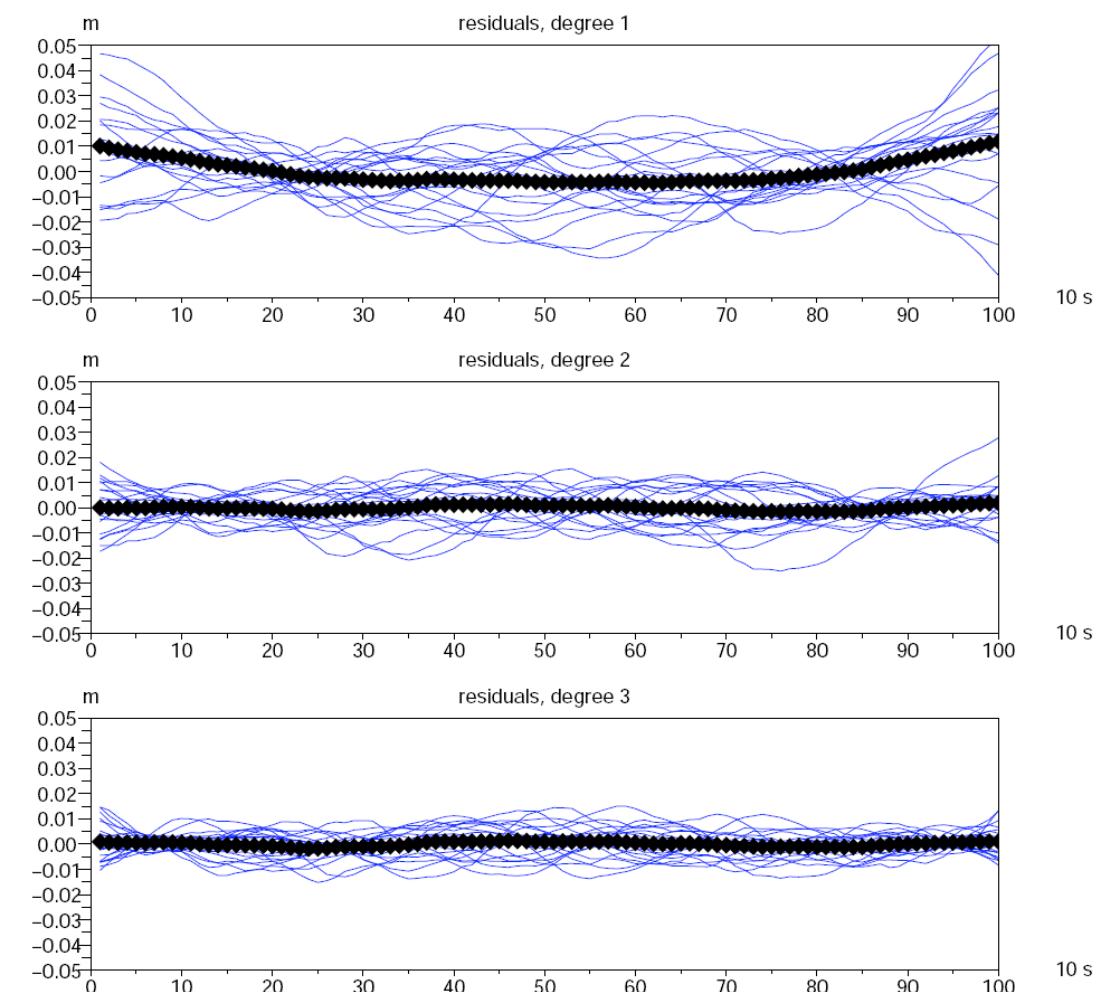
Phase processing : loss of observability due to interruptions

→ impossible to observe correctly low frequency evolutions

# Impact of clocks at 1000 sec time-scale

10 cm

Example: ground test of OUS  
 polynomial fit over 1000 s  
 impact of degree (1,2 or 3)  
 mean over 20 cases



To eliminate the impact of clocks :  
 - need to have many cycles  
 - use degree 3 polynomial

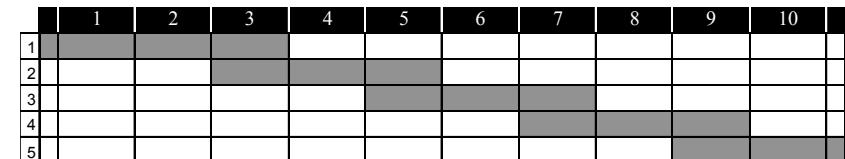
### Phase processing without cycle-slip reconstruction

- Pass-break introduced whenever a phase discontinuity(\*) occurs
- Phase discontinuities caused by near zero-doppler measurements are not considered
- Subsets left with < 10 valid measurements are rejected

Processing type	Doppler	Phase
Bias	-	1/set
Clock Drift	1/pass	1/set
Wet Zenith Delay	1/pass	1/set
Mean number of measurement per pass or set	68	49

(\*) Phase discontinuity: when the time interval between two valid measurements is greater than 10 sec.

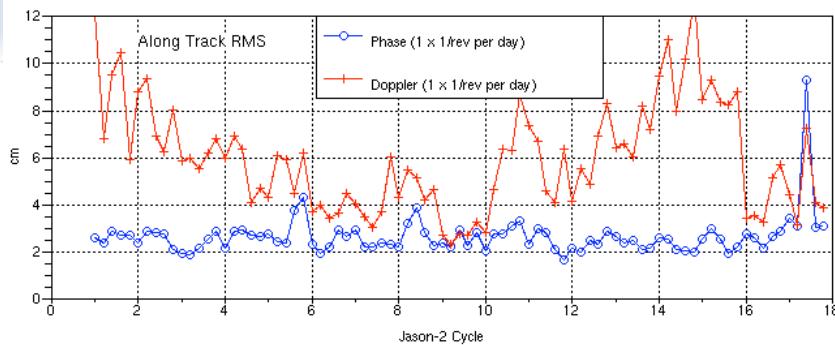
- ❑ Each 10-day cycle split into 5 arcs of about 3 days each with 1 day overlap
- ❑ About 35% of edited measurements
  - ♦ 20 % for cut-off angle = 10 deg.
  - ♦ 15 % usual editing of outliers  
(polynomial fit on doppler residuals)



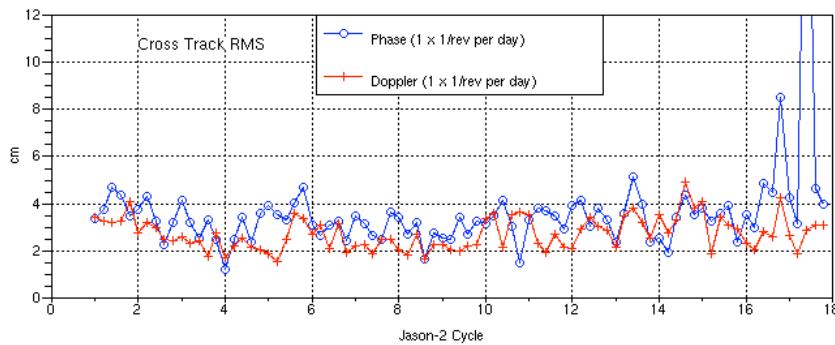
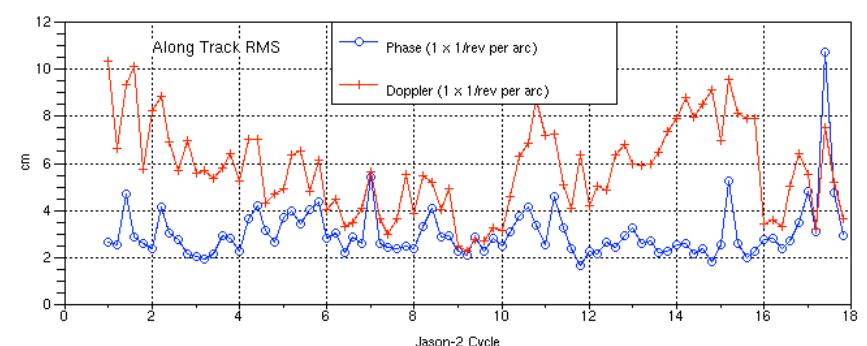
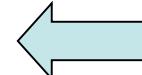
Arc number	Available measurements	Edited measurements		Valid passes	
		Doppler	Phase	Doppler	Phase
1	88612	30169	30556	861	1190
2	79033	27312	27738	762	1048
3	78554	26867	27442	768	1064
4	77806	26520	27090	761	1056
5	47467	16309	16631	461	626

# POD results using phase measurements

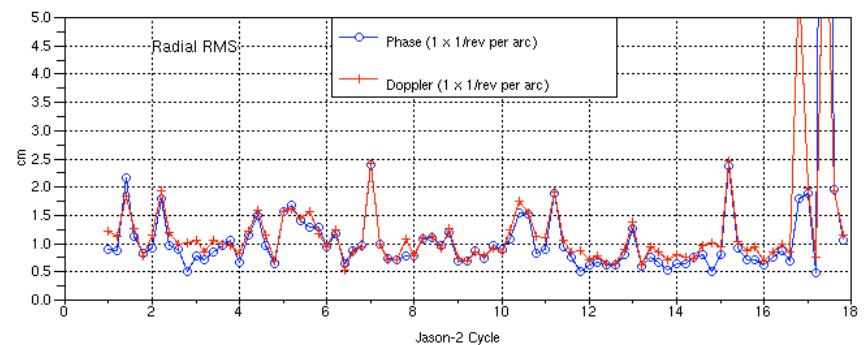
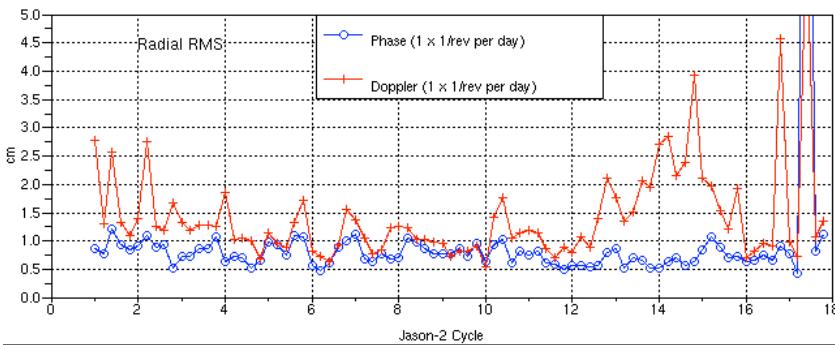
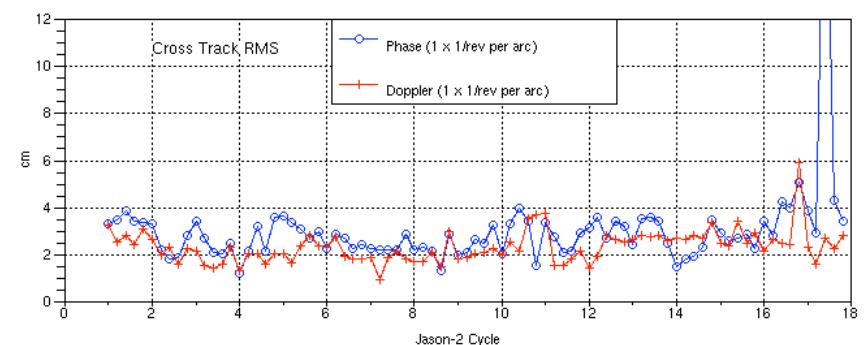
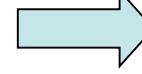
## Comparison to CNES D/L/G POE



1 along-track 1/rev per day

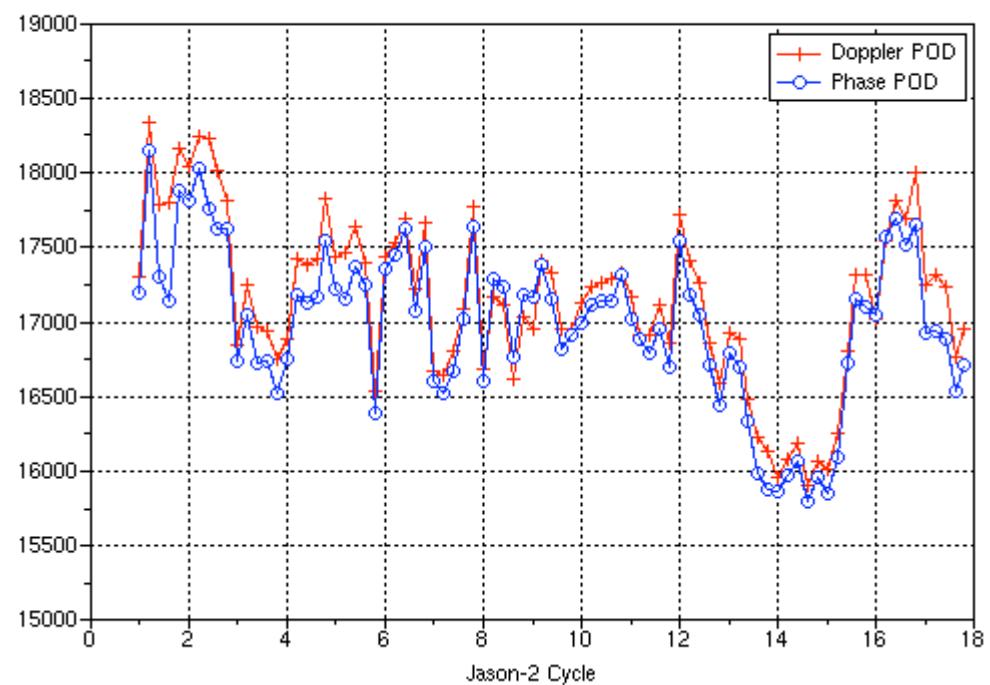
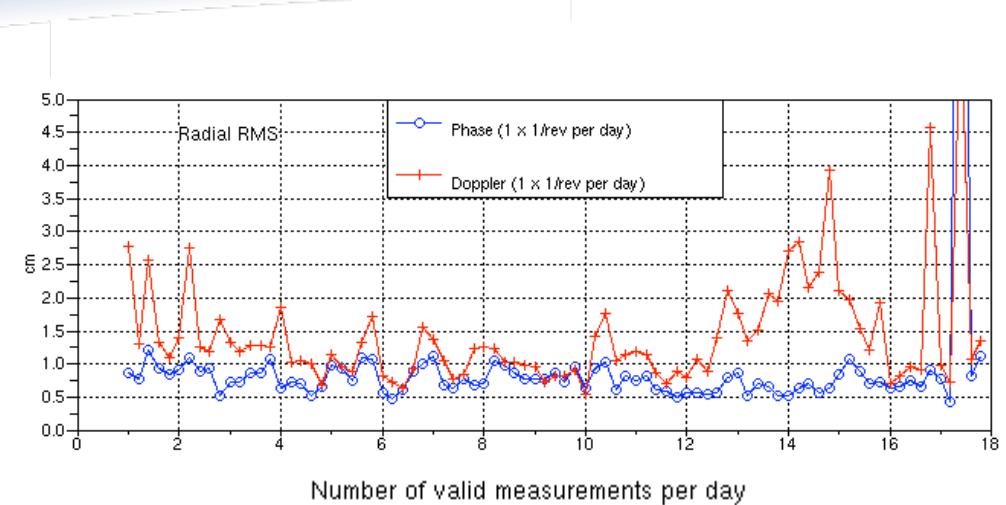


1 along-track 1/rev per arc

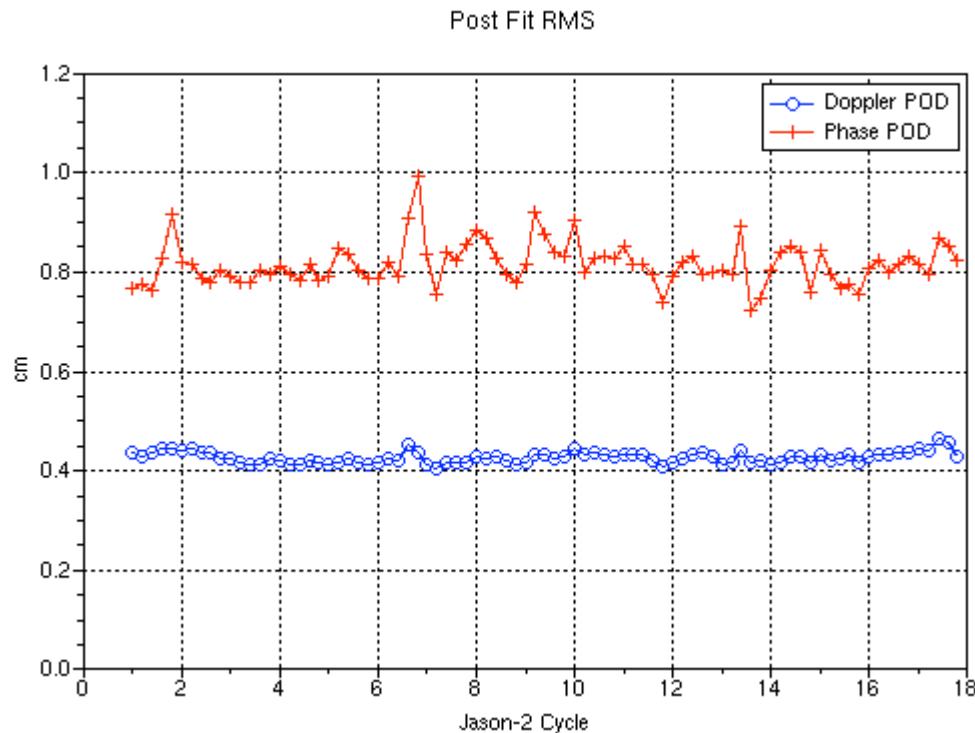


# POD results using phase measurements

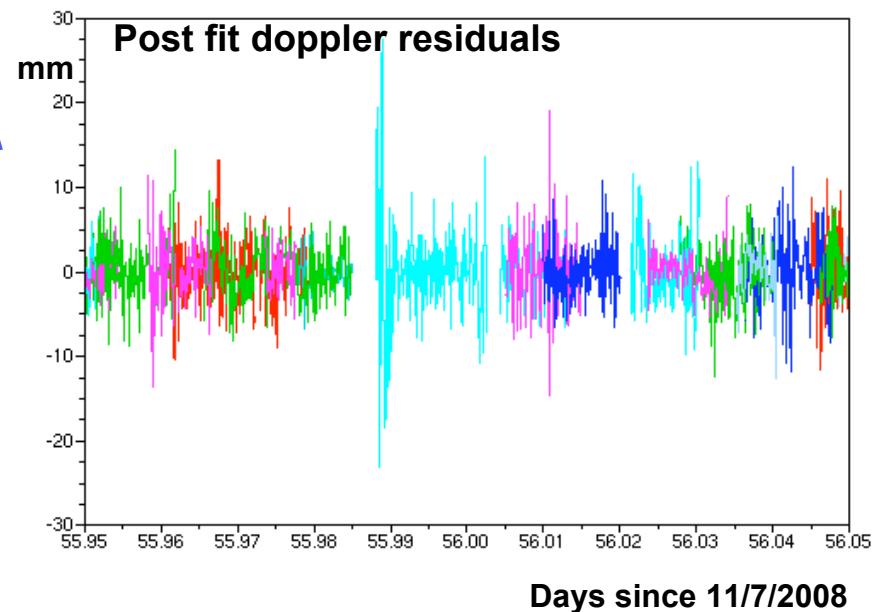
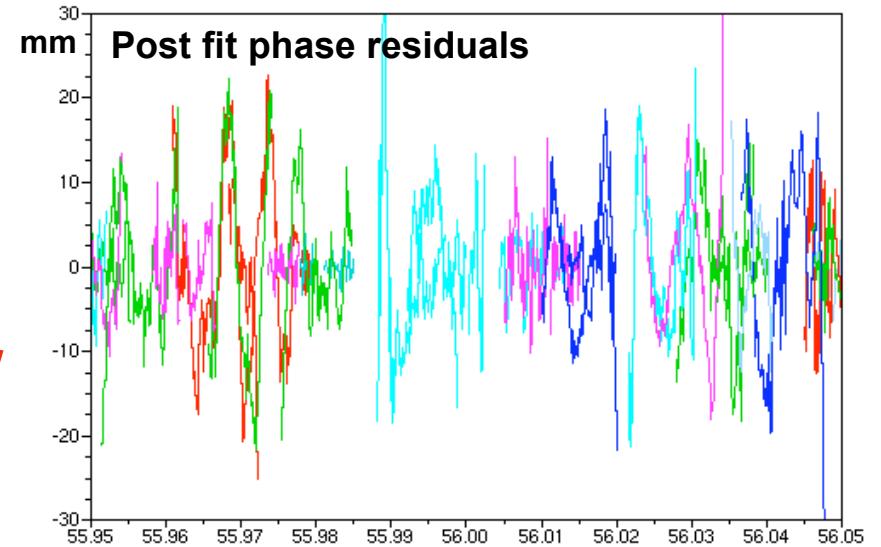
- 1/rev-per-day Doppler arcs much more affected by small variations of the measurements density
- Very stable performance of phase arcs, without needing any particular intervention



# Post-fit residuals

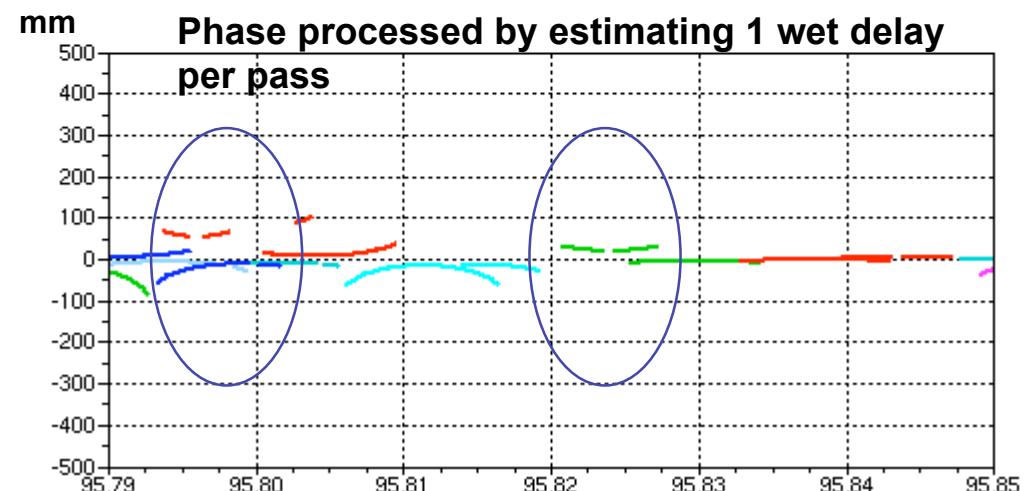
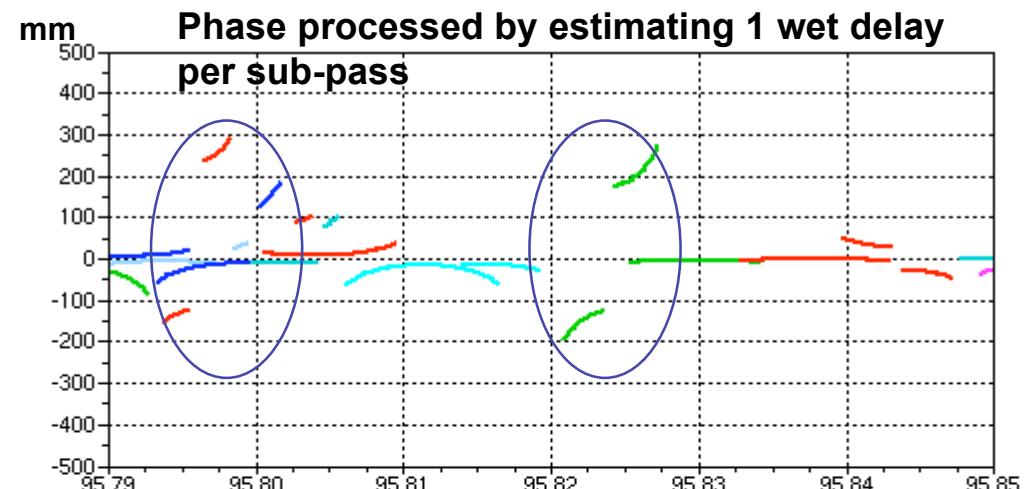


**Doppler measurements residuals are less dependent on clock behaviour at the pass time-scale**



### Comparison of doppler and phase tropospheric corrections after estimation of wet zenith delay

- The difference usually below 10 cm; can be much higher when the tropospheric bias gets correlated with clock offset
- This happens for short sub-passes
- Test performed by adjusting the phase troposphere over one full pass, like for doppler
- Resulting tropospheric delay is more consistent between doppler and phase
- No impact on the orbit (see backup slide)
- But what about positioning ?



- Analisys of phase residuals allows to clearly observe interference patterns and build phase maps for all the stations of the network
- It would not be realistic to correct these effects using maps obtained by phase residuals.
  - ◆ only visible effect would probably be to reduce RMS
  - ◆ but with the risk to introduce undesired biases in the solution
- Clocks' behaviour at 1000 sec. time scale is responsible for a large part of the post-fit phase residuals
- Orbits obtained by directly processing phase instead of doppler measurements can benefit from a significant gain in observability, without any observed impact of the aforementioned clock error
- Station positioning using phase measurements needs to be performed and investigated

# Backups

Résidus de la combinaison  $5L_1 - L_2$  (contribution iono très faible, mais 5 fois le bruit L1)

-saut proche d'un multiple de 5 ( typiquement  $k*5+[-0.25,0.25]$  avec  $k>1$  )

correction de L1

permet de traiter simplement les sauts fréquence centrale

-les sauts restants sont tels que :

$k$  cycles L1 et  $5k$  cycles L2 simultanés

donc détection sur L1 (1 cycle) ou L2 (5 cycles)

(performances similaires, moins de bruit sur L2)

Remarque :

si trop d'effet ionosphérique, remonter les seuils, il peut rester  $k=1$

$$\frac{\gamma\lambda_1 - 5\lambda_2}{\gamma - 1}$$

fait un saut de 2.2 mm sur la combinaison iono-free :

effet acceptable :

probabilité de beaucoup de cycles L2 vers le milieu du passage faible

biais de 2.2 mm en extrémité de passage non important devant les autres effets (horloges..)

# Sauts de phase et interruptions

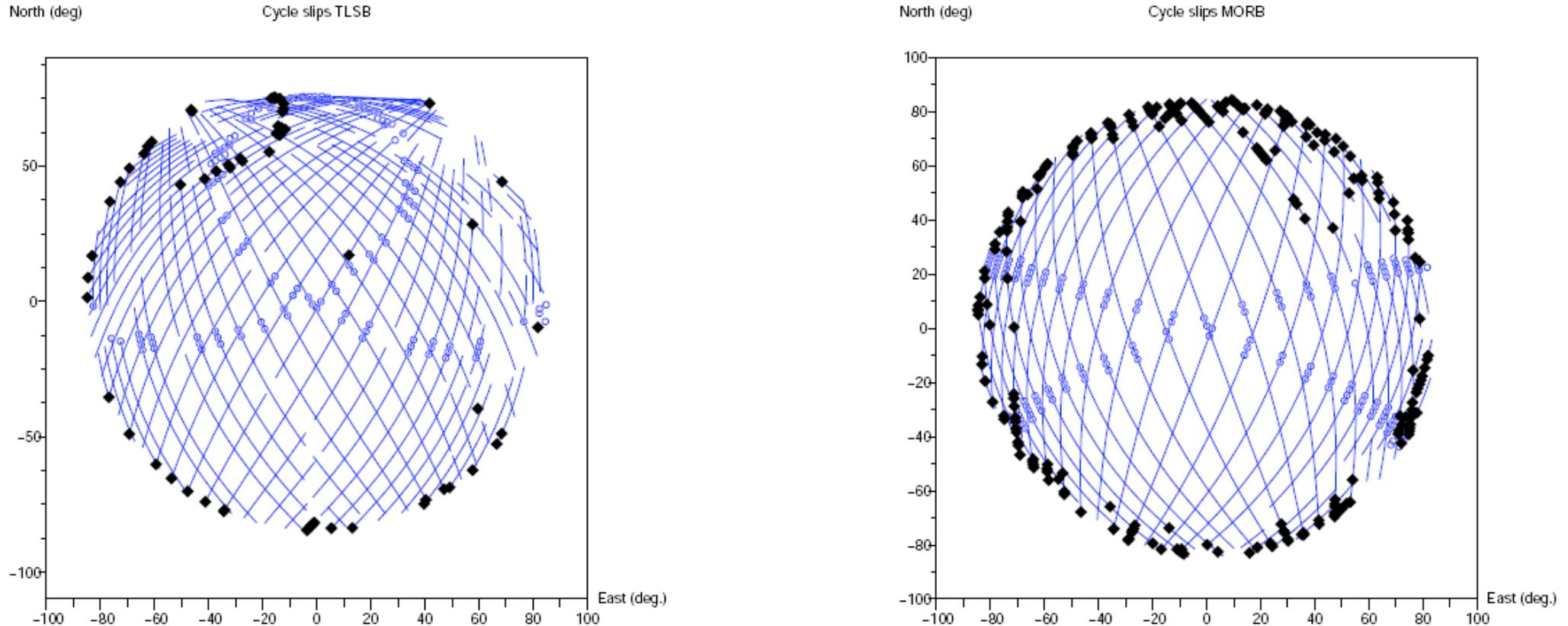


Figure 6: Cycle slips stations TLSB and MORB, with reconstruction

NOMBREUSES INTERRUPTIONS NON RECONSTRUCTIBLES SUR TLSB

# Estimation qualitative des interférences (1)

Objectif : comprendre les diamètres des cercles observés

400 MHz ou 2 GHz (plutôt du 2 GHz à cause de la combinaison iono-free ?)

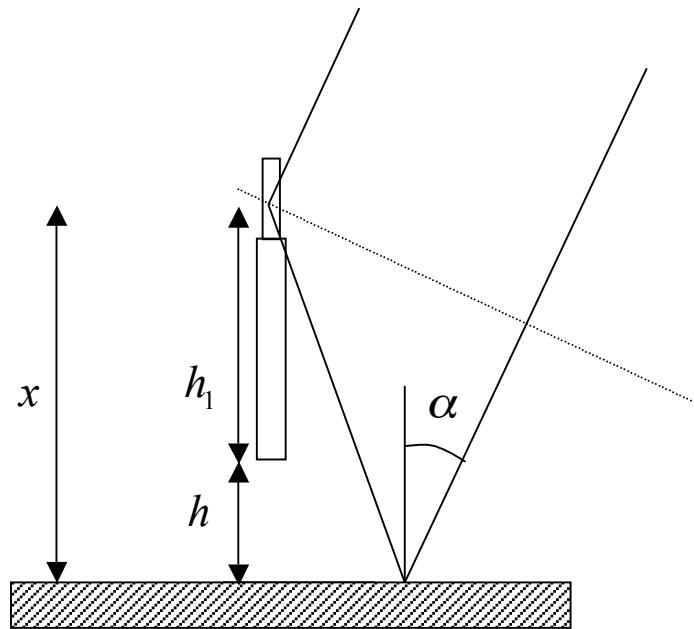
Différence de marche entre direct et réfléchi :

$$\frac{x}{\cos(\alpha)} + \frac{x}{\cos(\alpha)} \cos(2\alpha) = 2x \cos(\alpha)$$

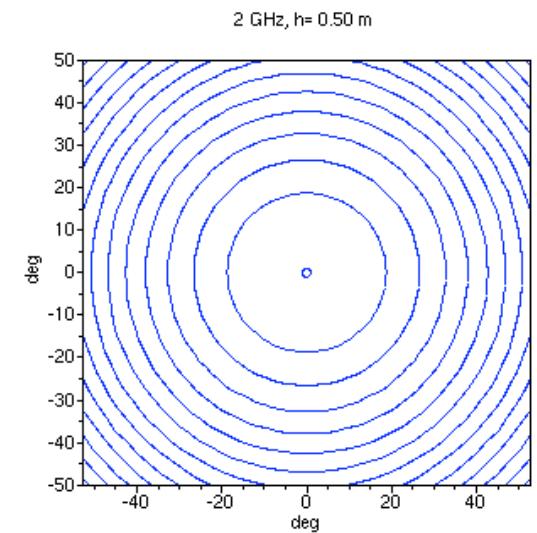
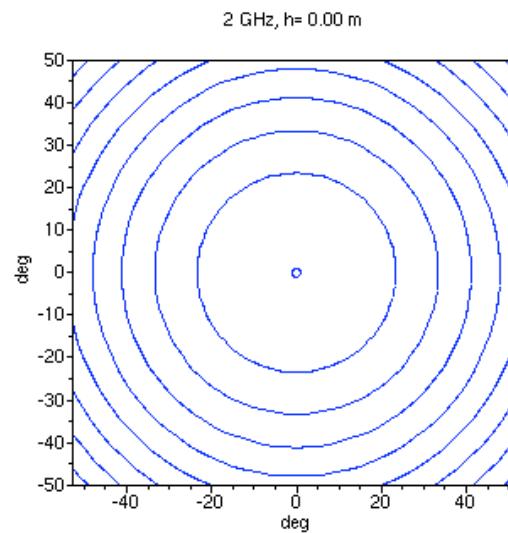
Variations par rapport au signal dans l'axe (2 GHz) :

$$k = \frac{2(h + h_1)(\cos(\alpha) - 1)}{\lambda_1}$$

$h$  : hauteur de la base



une analyse RF plus fine serait très intéressante  
(effet du montage de l'antenne ?)

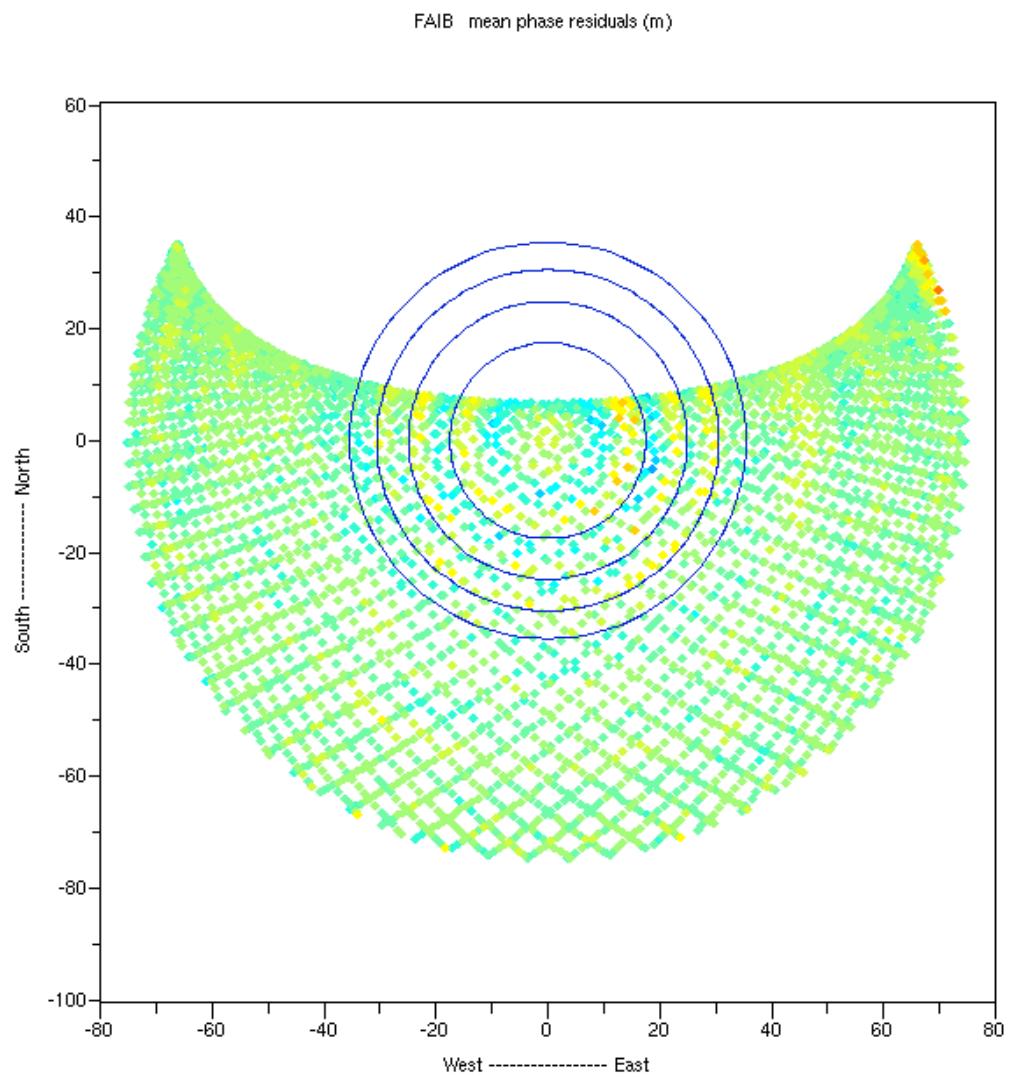


# Estimation qualitative des interférences (2)

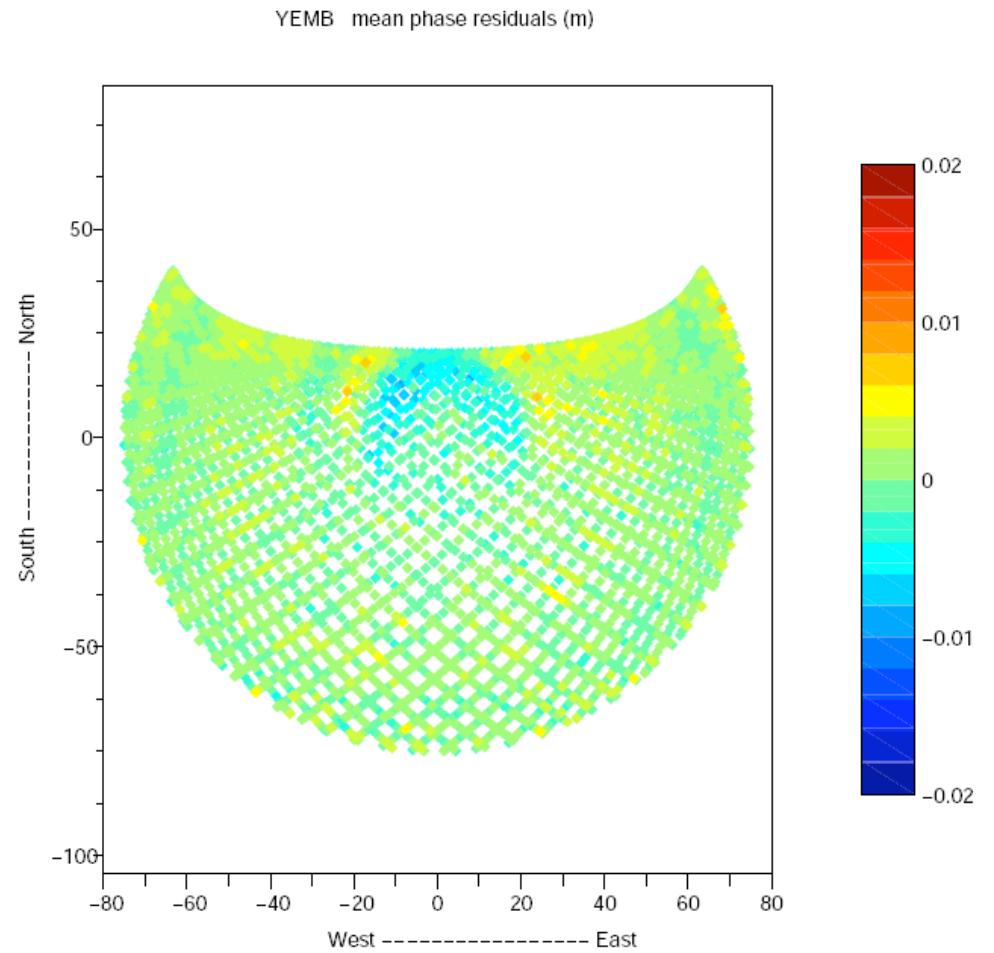
Fairbanks

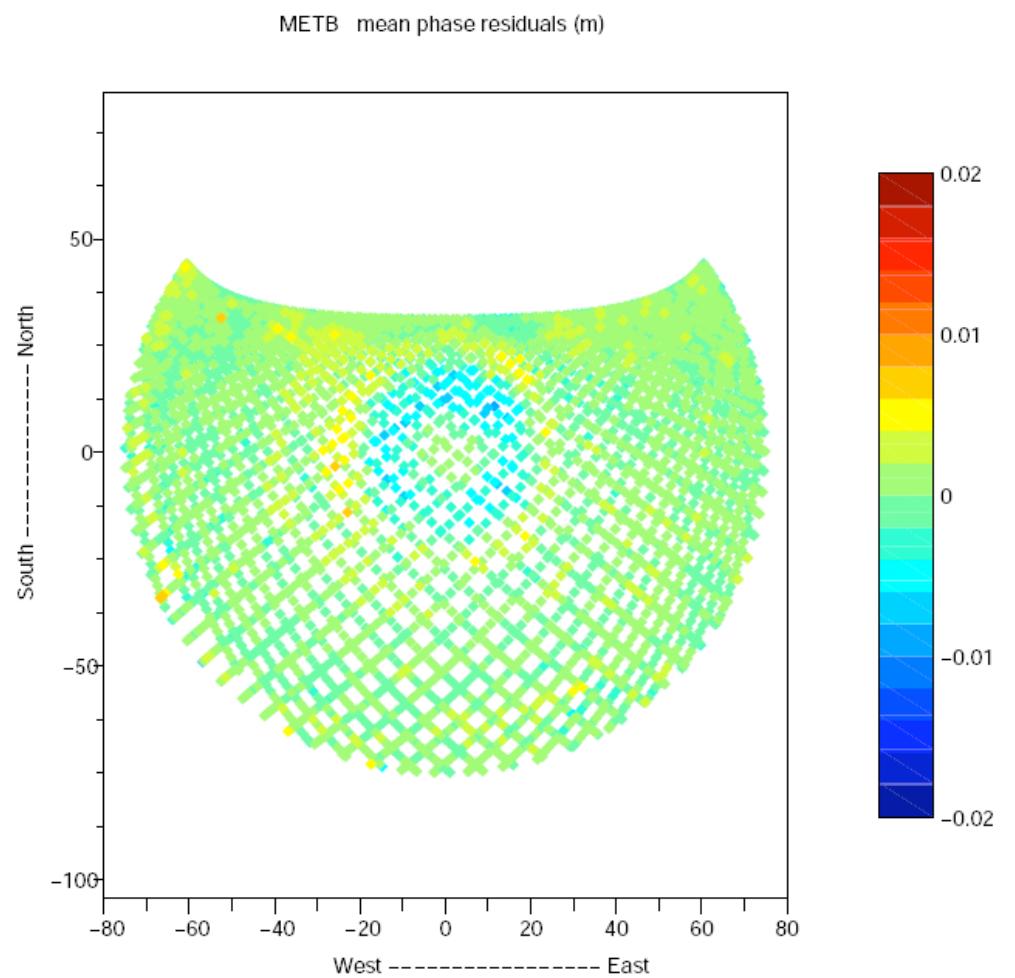
Calcul sur Fairbanks :  $h=0.7$  m

- cercles principaux dus au 2 GHz
- grands cercles (vers 45 degrés)  
400 MHz ?

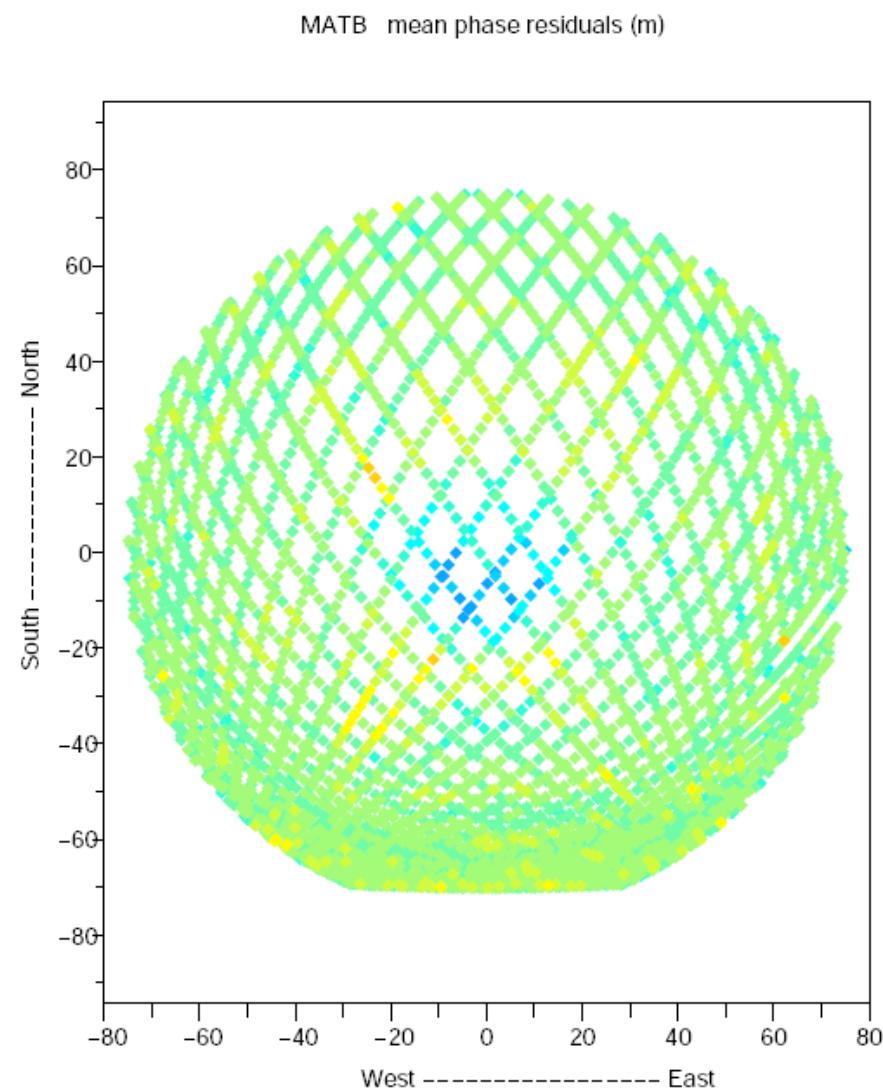


## Autres cartes, Yellowknife





## Autres cartes, MATB



La mesure de phase permet de construire des cartes de résidus de phase

- observation des interférences dans l'axe des antennes
- pas de limitation sur la géométrie des passages
- les effets d'horloge sont gênants

### Observation de multitrajets dans l'axe des antennes sur beaucoup de stations

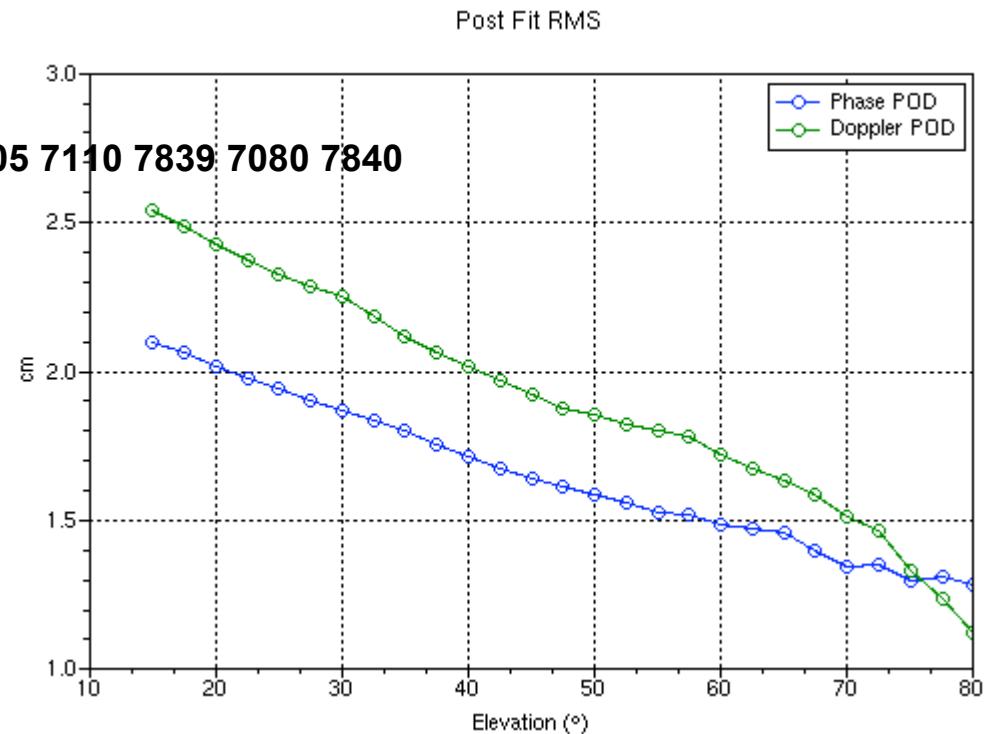
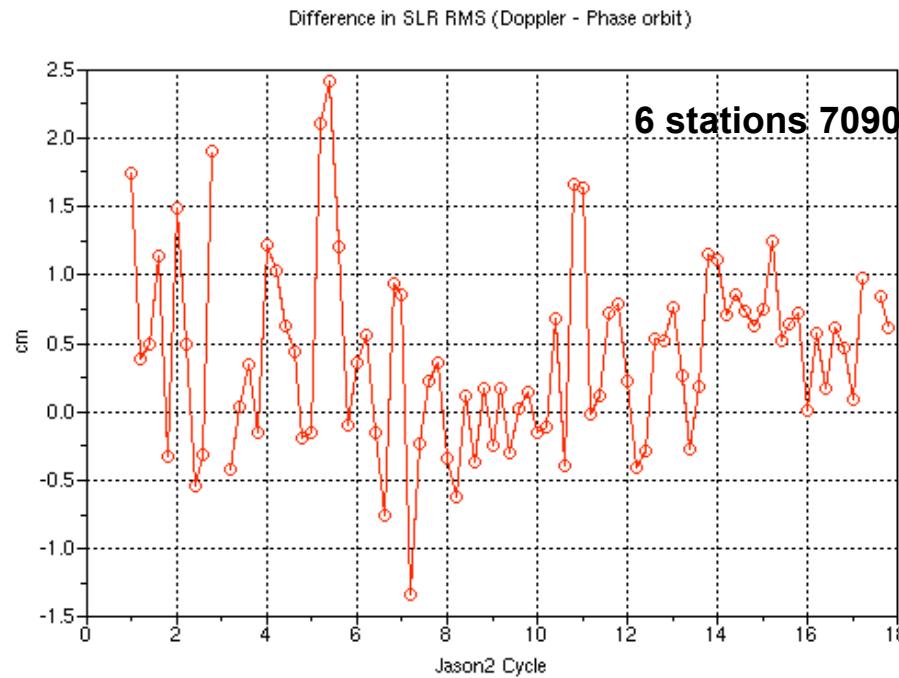
- termes de bas degré inobservables (en particulier termes paraboliques)
- comportement axisymétrique marqué
- anneaux concentriques sur certaines stations, erreurs max +-2 cm
  - plus faciles à observer aux latitudes élevées (densité des mesures)  
ADFB, FAIB, METB, RESB, YEMB
- résultats excellents sur certaines stations (AMUB)
  - donc probablement peu d'effets dus à Jason 2
- sur beaucoup de balises tendance à avoir un 'creux' au milieu (entre 0 et 20 degrés)
  - configuration balise ? influence du paramétrage (tropo, degré polynôme...) ?
- il ne serait pas réaliste de corriger ces effets par des cartes identifiées sur ces résidus
  - seul effet significatif : diminuer les rms
  - risque d'introduire des biais indésirables
- les cartes Jason2 sur l'ensemble du réseau, cycles 1-17, ont été calculées,
  - document disponible
- en attendant Cryosat ...

Pour orbitographie/positionnement : paramétrage plus complexe pour la phase par rapport au Doppler

- ambiguïté par paquet de phase continue
- troposphère par passage en visibilité
- effets de l'horloge : ajuster uniquement le biais de fréquence laisse des signatures paraboliques pouvant atteindre quelques centimètres
  - impacts sur le positionnement des stations ?

## Résidus laser sur orbites DORIS (Doppler / Phase)

- Dégradation des orbites doppler le long de la trace visible dans le résidus laser
  - ◆ Analyse sur la meilleure série Doppler ( 1 période de Hill / arc) et la meilleure série Phase (1 période de Hill / jour)



- Augmenter le nombre d'allongements tropo (découpage des visibilités) ne

Comparaison entre la solution de phase avec estimation d'un allongement tropo par sous-passage et une avec un allongement tropo par passage

